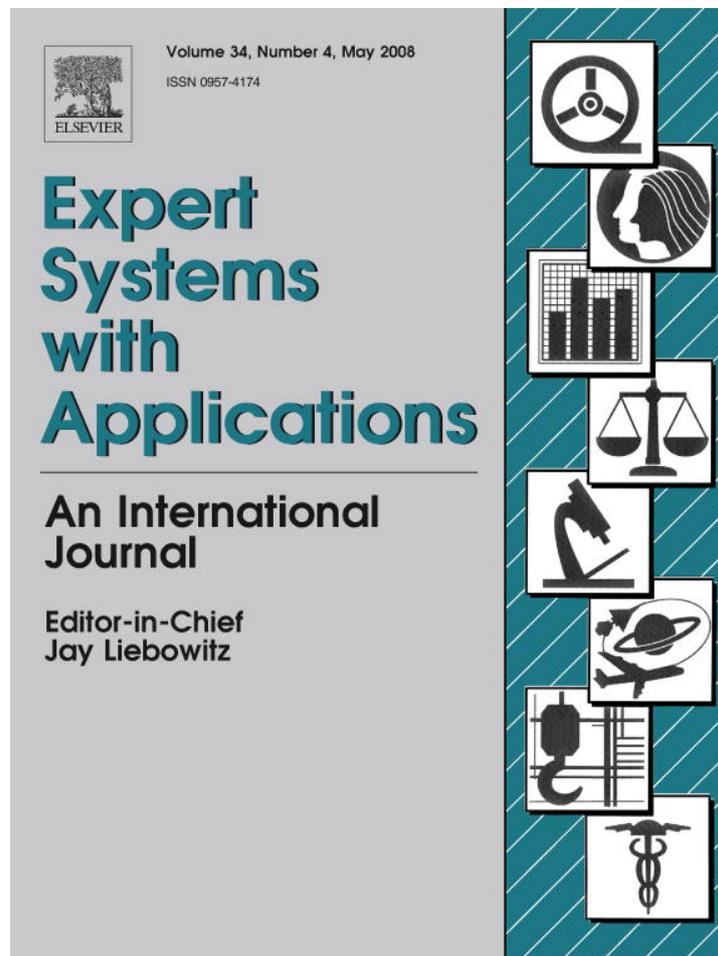


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# Adaptive wavelet network for multiple cardiac arrhythmias recognition

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## Abstract

This paper proposes a method for electrocardiogram (ECG) heartbeat detection and recognition using adaptive wavelet network (AWN). The ECG beat recognition can be divided into a sequence of stages, starting with feature extraction from QRS complexes, and then according to characteristic features to identify the cardiac arrhythmias including the supraventricular ectopic beat, bundle branch ectopic beat, and ventricular ectopic beat. The method of ECG beats is a two-subnetwork architecture, Morlet wavelets are used to enhance the features from each heartbeat, and probabilistic neural network (PNN) performs the recognition tasks. The AWN method is used for application in a dynamic environment, with add-in and delete-off features using automatic target adjustment and parameter tuning. The experimental results used from the MIT-BIH arrhythmia database demonstrate the efficiency of the proposed non-invasive method. Compared with conventional multi-layer neural networks, the test results also show accurate discrimination, fast learning, good adaptability, and faster processing time for detection.

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*Keywords:* Electrocardiogram (ECG); Adaptive wavelet network (AWN); Cardiac arrhythmia; Morlet wavelet; Probabilistic neural network (PNN)

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## 1. Introduction

Bio-signals on the surface of the human reflect the internal status and electric activity, thus providing information on internal organs with non-invasive measurement such as ECG, echocardiogram, or scintigraphy (Chen, Chen, & Tsai, 1997; Silipo & Marchesi, 1998). ECG has commonly used to collect large amounts of measurements that contain particular information in the signals. The typical diagnostic method is off-line analysis from the recorded data, and using a cardiogram to identify arrhythmic types of the patients. Designing non-invasive tools, abnormal monitoring techniques, signal processing, and classification capability for stationary/portable instruments has become an essential task. In addition, further integrating several techniques such as data analysis, pattern detection and discrimination, decision support, and human computer interface

is also necessary (Dickhaus & Heinrich, 1996; Qin et al., 2003). To ensure accurate detection, the algorithm requires real-time automatic classification, non-invasive, high-performance computing technique, reliable solutions, and simple for diagnosing disturbances of cardiac rhythm.

Diagnostic approaches have been applied to detection with frequency-domain and time-domain techniques. The QRS complex in ECG signals varies with the origination and the conduction path of the activation pulse in the heartbeat. When the activation pulse does not travel through the normal conduction path, the QRS complex becomes wide, and high-frequency components are attenuated. Power spectra of individual QRS complex are found at frequencies between 4 Hz and 20 Hz (Minami, Nakajima, & Toyoshima, 1999). With the time-domain technique, various features from each heartbeat are extracted to detect arrhythmia waveforms, such as width, height, area of QRS complex, and QRS morphology, etc. (Osowski & Linh, 2001). Applying these particular features, artificial intelligence (AI) approaches are used to perform ECG beat recognition. Various architectures for artificial neural networks (ANN) are

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used in this research, such as wavelet neural networks (Dickhaus & Heinrich, 1996), back-propagation networks (Acharya, Kumar, Bhat, Lim, & Lyengar, 2004; Minami et al., 1999; Silipo & Marchesi, 1998), Fuzzy hybrid neural networks (Osowski & Linh, 2001; Wang, Zhu, Thakor, & Xu, 2001), self-organizing map network (Hu, Palreddy, & Tompkins, 1997).

To develop a diagnostic method for arrhythmia classification, signal analysis based on wavelet transform (WT) has been presented to extract the characteristics of ECG signals (Dickhaus & Heinrich, 1996; Qin et al., 2003). The wavelet coefficients represent measures of similarity of the local shape of the signal to the mother wavelet under different dilation and translation parameters. This analysis is robust to time-varying signal analysis and it can point out occurrence time, but it is not capable of recognition. With multiresolution and localization of the wavelets (Lin & Wang, 2006) and pattern recognition capability of the ANN, wavelet network (WN) has become important for signal analysis and pattern recognition. When WN is applied in the real world, for example, the morphology variations of ECG waveforms are different for different patients, and even for the same patient or for the same type (Osowski & Linh, 2001), traditional networks can become a bottleneck requiring retraining with new features added into the current database. PNN (Specht et al., 1988) and general regression neural networks (GRNN) (Masters & Land, 1997; Seng et al., 2002) have been presented, and are recognized as having expandable or reducible network structure, fast learning speed, and promising results. In these adaptation methods, the choice of smoothing parameter has significant effects on the network outcome, and the choice of parameter is usually based on the overall statistical calculation from pre-collected training data. A dynamic model needs a non-statistical method as well as automatic adjustment of the targets and smoothing parameters for dynamic process technique (Masters & Land, 1997; Seng et al., 2002).

In this paper, AWN is proposed to recognize normal beat and six cardiac arrhythmias. The WN consists of two subnetworks connected in cascade. In the wavelet layer, the activation functions take the Morlet wavelets and are responsible for extracting features from each ECG signal. Subsequently, the PNN is an adaptive network with automatic tuning parameters and is used to classify cardiac arrhythmias. The results show computational efficiency and accurate recognition.

## 2. Adaptive wavelet network (AWN)

### 2.1. Morlet wavelet

In applications of signal analysis, it is necessary to extract signal features. Fourier analysis consists of breaking up a signal into sinusoidal waves of various frequencies, but it is only a time-domain transform, which has no time–frequency localization features. Similarly, wavelet analysis

is the breaking up of a signal into dilations and translation versions of the original wavelet, referred to as the mother wavelet. The wavelets must be oscillatory, have amplitudes that quickly decay to zero, and have at least one vanishing moment. The Morlet wavelet is the modulated Gaussian function, the family function is built starting from the following complex Gaussian function (Lin & Wang, 2006)

$$\psi(x) = \left( e^{j\omega_0 x} - e^{-\frac{\omega_0^2}{2}} \right) e^{-\frac{x^2}{2\sigma}}, \quad \sigma > 0. \quad (1)$$

The Fourier transform of  $\psi(x)$  is

$$\hat{\psi}(\omega) = \sqrt{2\pi\sigma} \left[ e^{-\frac{(\omega-\omega_0)^2}{2\sigma}} - e^{-\frac{\omega_0^2}{2}} e^{-\frac{\omega^2}{2\sigma}} \right]. \quad (2)$$

Let  $\omega = 0$ ; then  $\hat{\psi}(0) = 0$ , that is  $\int_R \psi(x) dx = 0$ , which represents the collection of all measurable functions in the real space, and  $\psi(x)$  satisfies the admissibility condition. When  $\omega_0 \geq 5$ , the appropriate Morlet wavelet becomes

$$\begin{aligned} \varphi(x) &= e^{j\omega_0 x} e^{-\frac{x^2}{2\sigma}} = [\cos(\omega_0 x) + j \sin(\omega_0 x)] e^{-\frac{x^2}{2\sigma}} \\ &= \varphi_R(x) + j\varphi_I(x), \quad \omega_0 \geq 5, \quad \sigma > 0, \end{aligned} \quad (3)$$

where  $\varphi_R(x)$  and  $\varphi_I(x)$  are the real and imaginary part respectively. Morlet wavelet is modulated Gaussian function by cosine. It has a better time–frequency localization feature and smoothes noise interference. When  $\varphi(x) \in L^2(\mathbb{R})$ , then mother wavelet becomes the daughter wavelet  $\varphi_{d,t}(x)$  with dilation parameter  $d$  and translation parameter  $t$ , as Eq. (4)

$$\begin{aligned} \varphi_{d,t}(x) &= \varphi_{R,d,t} \left( \frac{x-t}{d} \right) + j\varphi_{I,d,t} \left( \frac{x-t}{d} \right), \quad d \in \mathbb{R} \setminus \{0\}, \quad t \in \mathbb{R}, \\ \begin{cases} \varphi_{R,d,t}(x) &= \cos \left[ \frac{5(x-t)}{d} \right] e^{-\frac{(x-t)^2}{2\sigma d^2}}, \\ \varphi_{I,d,t}(x) &= \sin \left[ \frac{5(x-t)}{d} \right] e^{-\frac{(x-t)^2}{2\sigma d^2}}. \end{cases} \end{aligned} \quad (4)$$

Fig. 1 shows the wavelets with various dilation parameters ( $d = 1, 2, 3$ ) and translation parameters ( $t = -1, 0, 1$ ). In this study, both real and imaginary parts of the  $\varphi_{d,t}(x)$  can use to extract features from the ECG signals. Real part wavelets are applied to extract the features of normal beat (•) and cardiac arrhythmia disturbances including premature ventricular contraction (V), atrial premature beat (A), right bundle branch block beat (R), left bundle branch block beat (L), paced beat (P), and fusion of paced and normal beat (F). The activation functions of the wavelet nodes are derived from the mother wavelet  $\varphi_{di,t}(x_i)$  for  $i = 1, 2, 3, \dots, n$ , where  $n$  is the number of the wavelet nodes. The input vector  $X = [x_1, x_2, x_3, \dots, x_i, \dots, x_n]$  is connected to the WN, and inputs are the sample data from the QRS complexes as shown in Fig. 2.

### 2.2. Adaptive probabilistic neural network

Wavelets hybrid ANN is proposed to detect arrhythmia disturbances, and WN combines the properties of the

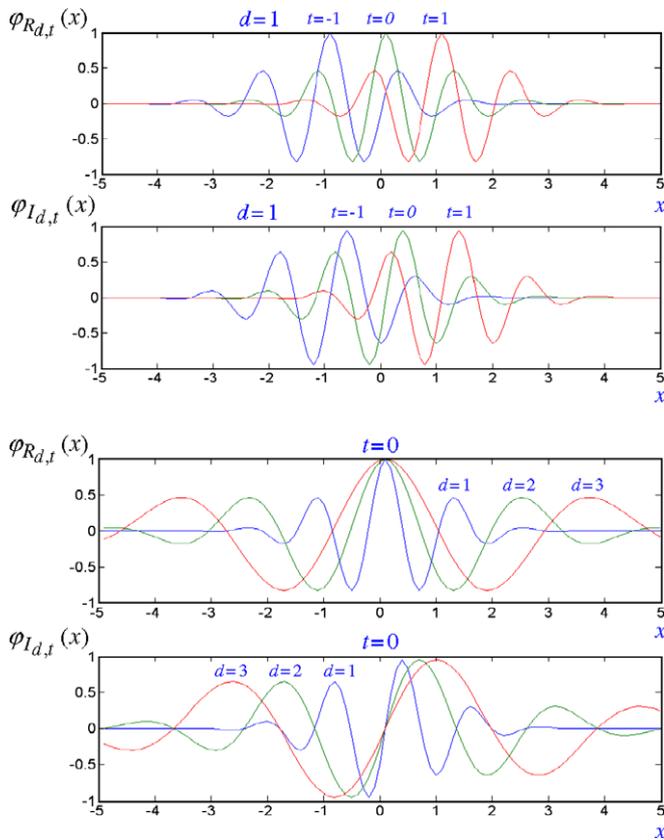


Fig. 1. The wavelets with various dilations and translations.

Morlet wavelets with the advantages of PNN. The second subnetwork with hidden, summation, and output layer is shown in Fig. 2. The number of hidden nodes  $H_k$  ( $k = 1, 2, 3, \dots, K$ ) is equal to the number of training examples, while the number of summation nodes  $S_j$  and output

nodes  $O_j$  ( $j = 1, 2, 3, \dots, m$ ) equals to the types of disturbances. The weights  $w_{ki}^{WH}$  (connecting the  $k$ th hidden node and the  $i$ th wavelet node) and  $w_{jk}^{HS}$  (connecting the  $j$ th summation node and the  $k$ th hidden node) are determined by  $K$  input–output training pairs. The final output of node  $O_j$  is (Masters & Land, 1997; Seng et al., 2002)

$$H_k = \exp \left[ - \sum_{i=1}^K \frac{(\varphi_i(x_i) - w_{ki}^{WH})^2}{2\sigma_k^2} \right], \quad (5)$$

$$O_j(\varphi) = \frac{\sum_{k=1}^K w_{jk}^{HS} H_k}{\sum_{k=1}^K H_k} = \frac{s(\varphi)}{h(\varphi)}, \quad (6)$$

where  $\sigma_1 = \sigma_2 = \dots = \sigma_k = \dots = \sigma_K$ . However, there are no means of generating an optimal smoothing parameter  $\sigma_k$ , and adjusting the  $\sigma_k$  would refine the accuracy in the dynamic environment. The optimal parameter  $\sigma_k$  is intended to minimize the object function, which is defined as squared error function  $e_j$  (Masters & Land, 1997)

$$e_j(\varphi, T) = [T_j - O_j(\varphi)]^2, \quad (7)$$

where  $T_j$  is the desired output for input vector  $X$ , and the implicit constraint is  $\sigma_k \neq 0$ . The first partial derivatives of error are shown in Eq. (8)

$$\begin{aligned} \frac{-\partial e_j(\varphi, T)}{\partial \sigma_k} &= 2[T_j - O_j(\varphi)] \frac{\partial O_j(\varphi)}{\partial \sigma_k} \\ &= 2[T_j - O_j(\varphi)] \left[ \frac{\frac{\partial s(\varphi)}{\partial \sigma_k} - O_j(\varphi) \frac{\partial h(\varphi)}{\partial \sigma_k}}{h(\varphi)} \right], \end{aligned} \quad (8)$$

$$\frac{\partial s(\varphi)}{\partial \sigma_k} = 2 \left[ \sum_{k=1}^K w_{jk}^{HS} H_k \right] \left[ \frac{(\varphi_i(x_i) - w_{ki}^{WH})^2}{2\sigma_k^3} \right], \quad (9)$$

$$\frac{\partial h(\varphi)}{\partial \sigma_k} = 2 \left[ \sum_{k=1}^K H_k \right] \left[ \frac{(\varphi_i(x_i) - w_{ki}^{WH})^2}{2\sigma_k^3} \right]. \quad (10)$$

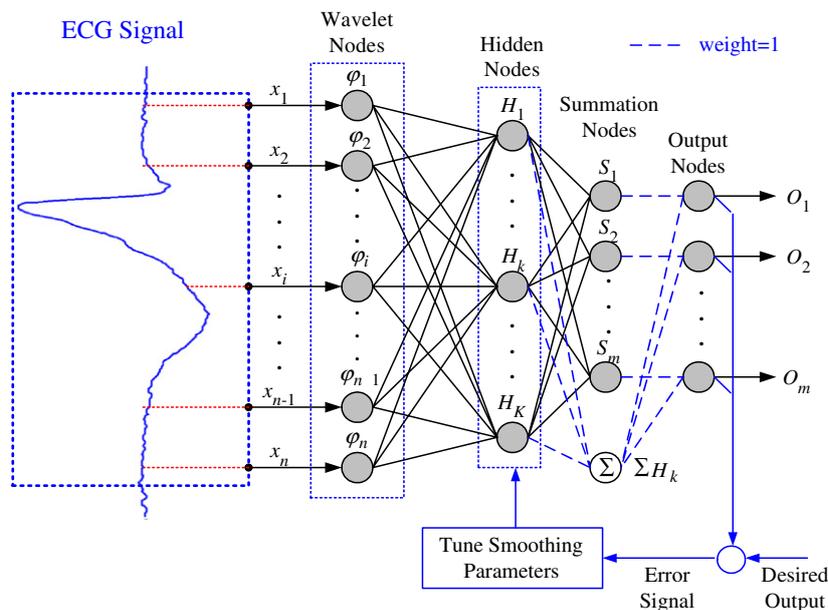


Fig. 2. Architecture of the adaptive wavelet network.

The gradient method is used to update parameter  $\sigma_k$  with iteration process, as in Eq. (11)

$$\sigma_k(p+1) = \sigma_k(p) + \eta \frac{\partial e_j(\varphi, T)}{\partial \sigma_k}, \quad (11)$$

where  $\eta$  is the learning rate, and  $p$  is the iteration number. In this study, AWN based algorithm contains two stages: the learning stage and recalling stage, as detailed below (Lin & Wang, 2006).

### 2.2.1. Learning stage

Step (1) For each training example  $X(k) = [x_1(k), x_2(k), \dots, x_i(k), \dots, x_n(k)]$  for  $k = 1, 2, 3, \dots, K$ , and  $i = 1, 2, 3, \dots, n$ , create weights  $w_{ki}^{WH}$  between wavelet node  $\varphi_i$  and hidden node  $H_k$  by

$$\begin{cases} \varphi_i(k) = \cos \left[ \frac{5(x_i(k) - t_i)}{d_i} \right] e^{-\frac{(x_i(k) - t_i)^2}{2\sigma d_i^2}}, \\ x_i = V(i), \quad t_i = V_{\text{nor}}(i) \end{cases}, \quad (12)$$

$$w_{ki}^{WH} = \varphi_i(k), \quad (13)$$

where  $d_i$  is the dilation parameters,  $d_i \in \mathbb{Z}$ ;  $x_i$  is a sequence of samples obtained from the QRS complex of unknown signal  $V$ ;  $t_i$  is the translation parameters, a sequence of samples obtained from the QRS complex of normal beat  $V_{\text{nor}}$ ;  $n$  is the number of sampling points; and  $W^{WH} = [w_{ki}^{WH}]$  is a  $k$  by  $n$  matrix.

Step (2) Create weights  $w_{jk}^{HS}$  between hidden node  $H_k$  and summation node  $O_j$  by

$$w_{jk}^{HS} = \begin{cases} 1 \\ 0 \end{cases} \quad (j = 1, 2, 3, \dots, m), \quad (14)$$

where the values of  $w_{jk}^{HS}$  are the predicted outputs associated with each stored pattern  $w_{ki}^{WH}$ , and  $W^{HS} = [w_{jk}^{HS}]$  is  $k$  by  $m$  matrix. Connection weights from hidden nodes  $H_k$  to summation node  $\sum$  are set 1.

### 2.2.2. Recalling stage

Step (1) Get network weights  $w_{ki}^{WH}$  and  $w_{jk}^{HS}$ .

Step (2) Apply test vector  $X = [x_1, x_2, x_3, \dots, x_i, \dots, x_n]$  to the AWN. Compute the output of wavelet node  $\varphi_i$

$$\varphi_i(x_i) = \cos \left[ \frac{5(x_i - t_i)}{d_i} \right] e^{-\frac{(x_i - t_i)^2}{2\sigma d_i^2}} \quad (15)$$

Step (3) Compute the output of hidden node  $H_k$  by using Eq. (5). The optimal value  $\sigma_k$  can be obtained by using Eqs. (8)–(11) based on minimum misclassification error (Convergent Condition: Infinity Norm).

Step (4) Compute the outputs of node  $O_j$  by using the Eq. (6).

## 3. Cardiac arrhythmias detection procedure

### 3.1. ECG characteristic and feature extraction

An ECG signal represents the changes in electrical potential during the heartbeat as recorded with non-invasive electrodes on the limbs and chest; a typical ECG signal consists of the P-wave, QRS complex, and T-waves. The P-wave is the result of slow-moving depolarization of the atria. The rapid depolarization of the ventricles results in the QRS complex of the ECG, which is a sharp wave about 1 mV amplitude and 80–100 ms duration. The plateau part of the action potential after QRS is called the ST segment (Silipo & Marchesi, 1998). The ECG waveform is the result of the potential change that propagates within the heart (electrical activity) and causes the cardiac muscle contraction, even varying with rhythm origin and conduction path. For example, when the activation pulse originates in the atrium and travels through the normal conduction path, the QRS complex has a sharp and narrow deflection, or else the QRS complex becomes wide and distorted (Minami et al., 1999). In the time domain, the normal beat and typical arrhythmia heartbeats are normalized as shown in Fig. 3. Each ECG signal has various morphological information and features, which can be used to classify seven categories.

The QRS complex of the ECG is important information in heart-rate monitoring and cardiac diseases diagnosis. The R-waves are detected by a peak detection algorithm, which begins by scanning for local maxima in the absolute value of ECG data. For certain window duration, the searching continues to look for a larger value. If this search finishes without finding a larger maximum, the current maximum is assigned as the R peak (Minami et al., 1999). Centered on the detected R peak, the QRS complex portion is extracted by applying a window of 280 ms, and P-wave and T-wave are excluded by this window duration. Based on 360 sampling rate, 100 samples can be acquired around the R peak (Sampling point  $n = 100$ , 50 points before and 50 points after). After sampling and performing analog-to-digital conversion, individual QRS complexes are extracted. The real part of wavelets  $\varphi_{Rd,t}(x_i)$ ,  $d = 3$ ,  $i = 1, 2, 3, \dots, 100$ , as Eq. (12), are responsible for extracting features under low frequency analysis, and these features are reconstructed by 100 wavelet nodes to form the symptomatic patterns, as shown in Fig. 4. For example, the symptomatic pattern of a normal beat has a near rectangular-impulse-sequence graph with amplitude one. The morphology of symptomatic patterns will reveal the serious dip and bumpy shapes for abnormal heartbeats. Symptomatic patterns of the same categories have similar morphology or multiform. The amplitudes having a specific dip range can be observed between zero and one in the rectangular section. According to the morphology, various patterns indicate different cardiac diseases. These symptomatic patterns are considered for training the AWN.

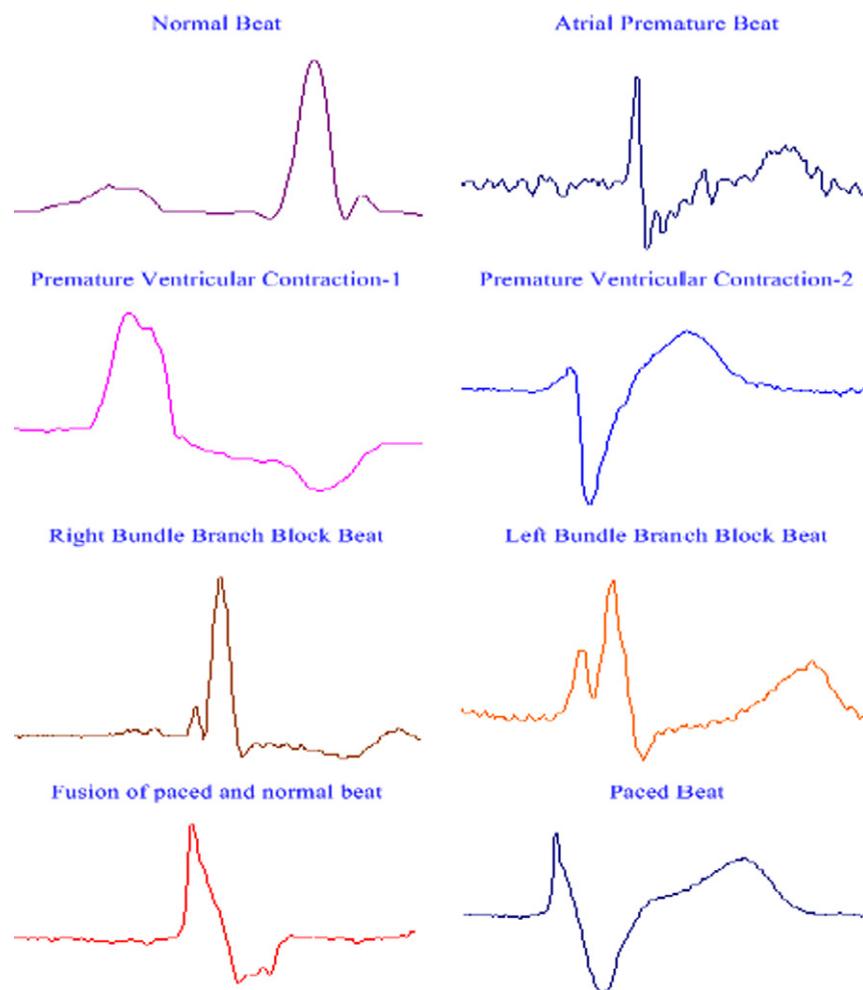


Fig. 3. Typical arrhythmia heartbeats in time domain (Lead II signal).

### 3.2. Training patterns creation

In this study, the dataset of QRS complexes typically for seven categories are taken from the MIT-BIH arrhythmias database (from Record 100 to Record 234) (Goldberger et al., 2000). The database contains 48 records, and each record is slightly over 30 min long. In most records, the upper signal is a modified limb lead II (ML II) and the lower signal is a modified lead V1 (VI). Seven heartbeat classes have been included in the investigations, involving normal beat, supraventricular ectopic beat, bundle branch ectopic beat, and ventricular ectopic beat as shown in Table 1 (Chazal, Dwyer, & Reilly, 2004). A total of 43 QRS complexes (ML II Signal) are selected including patient numbers 107, 109, 111, 118, 119, 124, 200, 209, 212, 214, 217, 221, 231, 232, and 233, and the templates of seven classes are produced by Eqs. (12) and (13). The numbers of symptomatic patterns from the same class are 7-, 11-, 2-, 7-, 8-, 6-, and 2-set data ( $K_{\text{nor}}=7$ ,  $K_V=11$ ,  $K_A=2$ ,  $K_L=7$ ,  $K_R=8$ ,  $K_P=6$ ,  $K_F=2$ ) respectively. Because the characteristics are enhanced, the number of training data requirements can be reduced. We can system-

atically create weights between wavelet nodes and hidden nodes with 43-set training data,  $k = 1, 2, 3, \dots, 43$ . The weights between hidden nodes and summation nodes are encoded as binary values by Eq. (14) with signal “1” for belonging to Class  $j$ ,  $j = 1, 2, 3, \dots, 7$ .

The AWN contains 100 wavelet nodes, 43 hidden nodes, eight summation nodes, and seven output nodes. The number of wavelet nodes is equal to the number of the sampling points, the number of hidden nodes is equal to the number of training data, and each output represents one normal beat and six types of arrhythmias as defining output vector  $O = [O_1, O_2, O_3, O_4, O_5, O_6, O_7] = [O_{\text{Nor}}, O_V, O_A, O_L, O_R, O_P, O_F]$ . The selection sort is applied to find the maximum value that indicates the arrhythmic type. The output values are between 0 and 1, where a value close to 1 means “Normal”, and close to 0 means “Abnormal”. If clinicians provide some suggestion or more patterns are generated in clinical investigation, training data can be continually added to the current database. The database can be enhanced at any time with new training data. The corresponding hidden nodes will continue to grow, and will update the network weights without re-iteration to corrupt

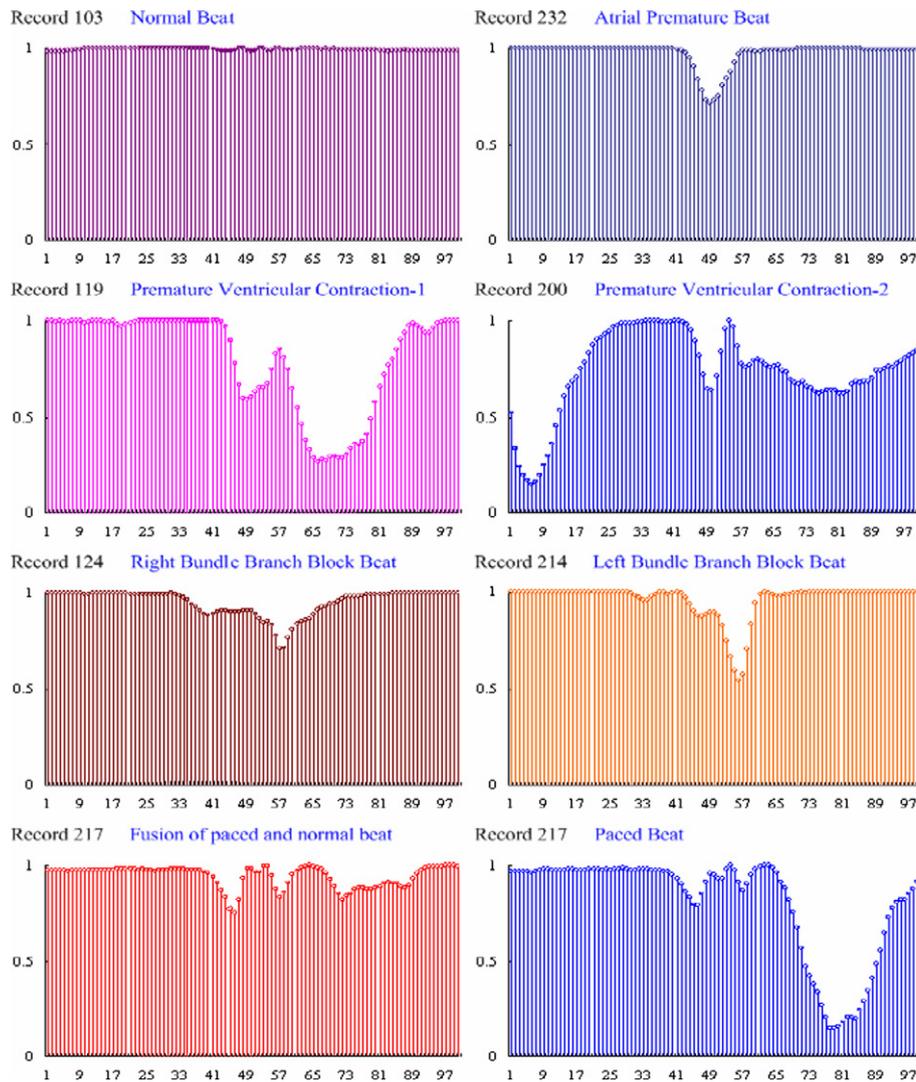


Fig. 4. Various symptomatic patterns in time-frequency domain.

the previous database or weights. This process results in very fast training, and the network is adaptive to data changes by tuning smoothing parameters.

#### 4. Experiment result

The proposed detection algorithm was developed on a PC Pentium-IV 2.4 GHz with 480 MB RAM and Matlab workspace, based on the MIT-BIH arrhythmias records. The performance of the proposed model was tested with learning performance for the training data and detection accuracy for the untrained data, as detailed below.

##### 4.1. Single cardiac arrhythmia with noise influence

In ECG measurement, signals may be disturbed by noise such as power line interference (Minami et al., 1999) or quantification error (Gaussian noises). The ECG signal

sometimes is disturbed by 50 Hz or 60 Hz interference whose amplitude is approximately 5–6 times less than the R-peak, as Fig. 5a shows the ECG signals of normal heart-beat and V in the time domain, and Fig. 5b shows the ECG signals with 60 Hz noise influences. Using 100 heartbeats (about 1.5 min long) of the patient numbers 119, 200, and 212 (Goldberger et al., 2000) containing normal beats, pattern  $V_s$ , and pattern  $R_s$ , the results show that high accuracies of the proposed algorithm, as shown in Table 2. Test 1 shows the test results without any noise, and Test 2 shows the results with presenting ECG signals involving 60 Hz interference. The proposed method is robust enough to handle noisy environments. Overall accuracies are greater than 90%. The positive predictivity of more than 80% is obtained to quantify the performance of proposed method with or without a noisy background. It can be seen that the features of heartbeats are still strong enough to recognize, and the symptomatic patterns are not corrupted by noise influences as shown in Fig. 6. When the symptomatic patterns have

Table 1  
Heartbeat types of human ECG data

Class	Beat	Symbol	Record	Patient
Normal	Normal beat	•	MIT-100	Male, age 69
			MIT-103	Male, age *
			MIT-119	Female, age 51
			MIT-200	Male, age 64
			MIT-209	Male, age 62
			MIT-212	Female, age 32
			MIT-221	Male, age 83
Ventricular ectopic beat	Ventricular premature contraction	V	MIT-119	Female, age 51
			MIT-200	Male, age 64
			MIT-221	Male, age 83
			MIT-233	Male, age 57
Supraventricular ectopic beat	Atrium premature beat	A	MIT-202	Male, age 68
			MIT-232	Female, age 76
Bundle branch ectopic beat	Left bundle branch block beat	L	MIT-109	Female, age 64
			MIT-111	Female, age 47
			MIT-207	Female, age 89
			MIT-214	Male, age 53
	Right bundle branch block beat	R	MIT-118	Male, age 69
			MIT-124	Male, age 77
			MIT-212	Female, age 32
			MIT-231	Female, age 72
Unknown	Paced beat	P	MIT-107	Male, age 63
			MIT-217	Male, age 65
Fusion beat	Fusion of paced and normal beat	F	MIT-217	Male, age 65

Note: \*: Not recorded.

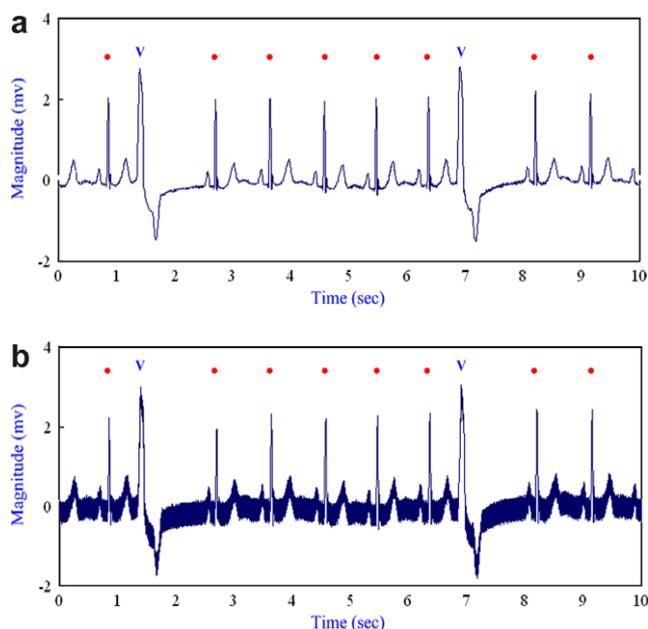


Fig. 5. ECG signals in time domain (Record 119) (a) ECG signals of normal beat and V; (b) ECG signals of normal beat and V with 60 Hz power line interference.

morphological variation or sag shapes, the critical times for starting and ending of occurrences are clearly noted, and the number of abnormal beats is easy to count. This study

Table 2  
The test results of single cardiac arrhythmias

Record		Number of arrhythmias						CPU time (s)	Accuracy <sup>a</sup> (%)
		•	V	A	L	R	P		
119	Actual	75	25	0	0	0	0	0	–
	Test1	75	25	0	0	0	0	0	0.096
	Test2	75	25	0	0	0	0	0	0.105
200	Actual	62	38	0	0	0	0	0	–
	Test1	62	35	0	1	2	0	0	0.109
	Test2	62	35	0	1	2	0	0	0.156
212	Actual	5	0	0	0	95	0	0	–
	Test1	9	0	0	0	91	0	0	0.109
	Test2	9	0	0	0	91	0	0	0.110

<sup>a</sup> Accuracy (%) =  $(N_r/N_t) \times 100\%$ ;  $N_r$ : the number of correctly discriminated beats;  $N_t$ : total number of heartbeats.

case confirms that the proposed method can work in an uncertain environment with a noisy background.

#### 4.2. Multiple cardiac arrhythmias

Some of the clinical cases include multiple cardiac arrhythmias, for example ventricular ectopic beat, bundle branch ectopic beat, fusion, and paced beats. Using 100 heartbeats of the patient numbers 217, 214, and 118 including multiple cardiac arrhythmias (Masters & Land, 1997),

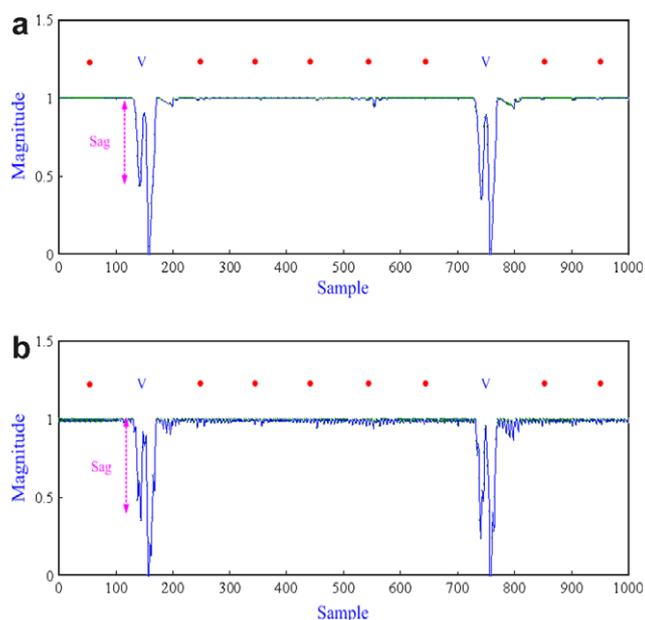


Fig. 6. Symptomatic patterns in time–frequency domain (a) symptomatic patterns of normal beat and *V*; (b) symptomatic patterns of normal beat and *V* with 60 Hz power line interference.

Test 1 and Test 2 show that the accuracies are greater than 90%, as shown in Table 3. The results confirm that the

Table 3  
The test results of multiple cardiac arrhythmias

Record		Number of arrhythmias						CPU time (s)	Accuracy <sup>a</sup> (%)	
		<i>V</i>	<i>A</i>	<i>L</i>	<i>R</i>	<i>P</i>	<i>F</i>			
217	Actual	0	3	0	0	0	94	3	–	94
	Test	0	4	0	0	1	88	7	0.113	
214	Actual	0	5	0	95	0	0	0	–	96
	Test	1	5	3	91	0	0	0	0.108	
118	Actual	0	1	0	0	99	0	0	–	94
	Test	4	1	0	2	93	0	0	0.111	

<sup>a</sup> Accuracy (%) =  $(N_r/N_t) \times 100\%$ ;  $N_r$ : the number of correctly discriminated beats;  $N_t$ : total number of heartbeats.

major types are paced beat (*P*), left bundle branch beat (*L*), and right bundle branch beat (*R*). Fig. 7 shows the traced detection results of patient number 118 and appears six misclassification errors ( $\oplus$ ) of class *R* in the output  $O_R$ . The processes recognized 94 paced beats with six failures, 95 left bundle branch ectopic beats with four failures, and 99 right bundle branch ectopic beats with six failures, respectively. The positive predictivity of more than 80% is also obtained to quantify the performance with or without a noisy background. Second study case confirms that the proposed method can detect multiple cardiac arrhythmias with high confidence.

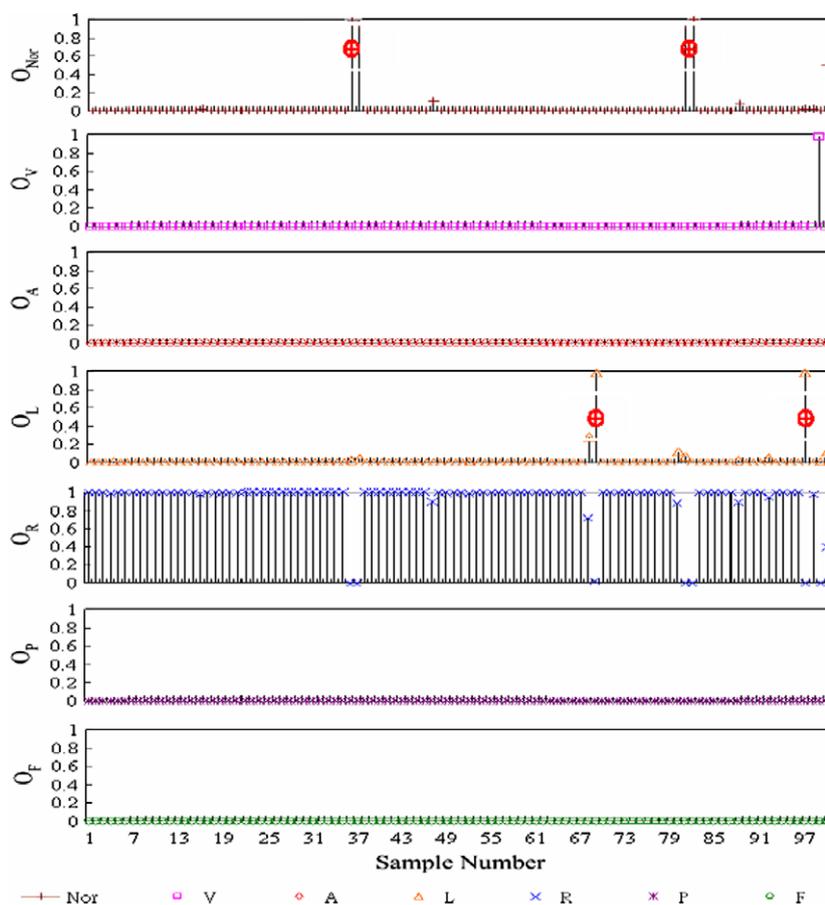


Fig. 7. Detection results of patient number 118. Note:  $\oplus$ : Error.

4.3. Learning performance tests

Figs. 8a and b show the squared errors and smoothing parameters versus learning cycles, respectively. The performance of AWN is affected by the width of the Gaussian activation function. As the width of Gaussian function decreases, decision boundaries can become increasingly nonlinear. For a very narrow Gaussian function, the network approaches a nearest-neighbor classifier (Lin & Tsao, 2005; Lin & Wang, 2006). Eqs. (8)–(11) are used to find near-optimum smoothing parameters that minimize the training-data error of the AWN as the number of training data increases from  $K_1=18$  to  $K_6=43$ . The corresponding hidden nodes will continue to grow from 18 to 43, and construct the network weights without any iteration process. This process results in very fast training, and the network is adaptive to match desired output with add-in/delete-off training patterns by tuning smoothing parameters for six learning stages. Learning rates  $\eta = 0.1-0.3$  are selected for training AWN as shown in Table 4. Fig. 8 shows the final squared errors after the training AWN has been responsible for the determining smoothing parameters. For the convergent condition  $e \leq 10^{-3}$ , AWN rapidly converges to the nearest local minimum for less than 40 learning cycles in a shorter processing time. It takes 0.782 s

Table 4  
Comparison of AWN with WBPB

Method	Network topology	Training patterns	Learning rate $\eta$	Learning cycles	Average CPU time (s)
*AWN	100-43-8-7	43	0.1–0.3	$\leq 40$	0.782
WBPB	100-100-27-7 100-100-54-7 100-100-107-7	43	0.2–0.8	<10000	<800

Note: (1)  $N_H = (N_I + N_O)^{1/2}$ ; (2)  $N_H = (N_I + N_O)/2$ ; (3)  $N_H = (N_I + N_O)$ .  $N_H$ : the number of hidden node;  $N_I$ : the number of input node;  $N_O$ : the number of output node.

(Average CPU Time) to classify the 43 training data into seven categories.

The output values of AWN are shown in Fig. 9a. AWN automatically adjusts outputs to approach the targets with tuning smoothing parameters in the learning stages. Threshold value 0.5 is used to separate “Normal” from “Abnormal”, and can correctly discriminate. The proposed method has the advantages of fast learning process, learning stage with slight iteration for updating weights, and adaptation capability. However, the performance is affected by the parameter of Gaussian activation function. For 43 trained data and 1200 untrained data including single and multiple cardiac arrhythmias, the ranges of parameters could be determined by experience and trial-and-error procedure with tuning parameters. The detection accuracy decreases as smoothing parameters increase. The choice of parameters will affect the estimation error, and the suitable range is from 0.05 to 0.30 for reducing misclassification errors, and the accuracies are greater than 90% as shown in Fig. 9b. Refining the parameters can enhance the detection accuracy by using the proposed optimum method. The near-optimal parameter  $\sigma = 0.078$  can minimize the classification error, and the accuracies are the maximums for single and multiple cardiac arrhythmias, as shown in Fig. 9b.

For comparison purposes, we have also applied the WBPB composed of 100 wavelet nodes in the wavelet layer and multi-layer neural network (MLNN). For the second subnetwork, a MLNN is used for training with the back-propagation learning algorithm. Only one hidden layer is used, and the number of hidden nodes is determined by the experience formulas as shown in Table 4. Traditional MLNN has some limitations including very slow learning process, needs iteration for determining weights and learning rates ( $\eta = 0.2-0.8$ ), and needs to determine the network architecture such as the number of hidden layers and hidden nodes, which is difficult to retrain with new training data. With various tests, we can see that the training time of AWN outperformed WBPB. AWN has a fast learning process needing no iteration for updating weights, a flexible hidden nodes mechanism with add-in or delete-off, and automatic adjustment of the targets and parameter  $\sigma$ . With the same training data, the proposed AWN shows better performance than WBPB as shown in Table 4.

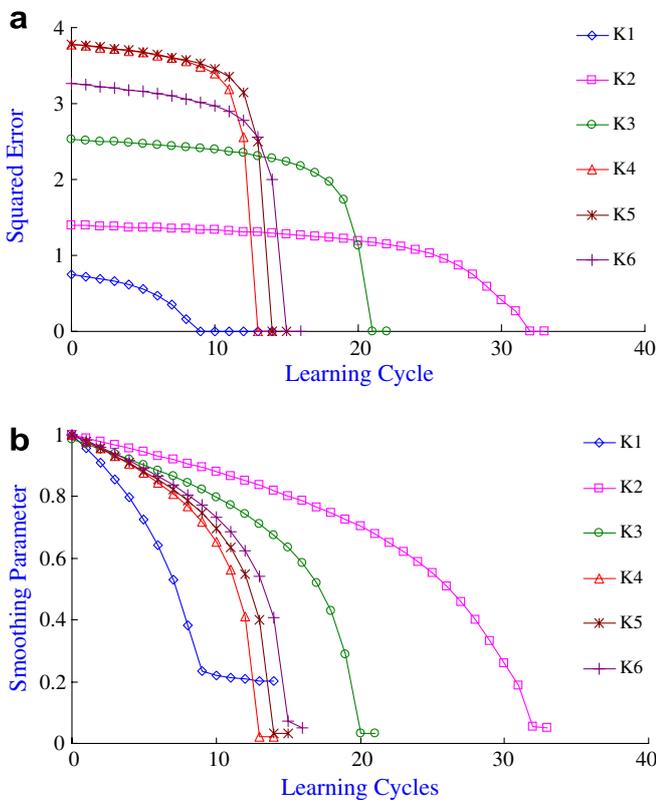


Fig. 8. (a) Squared errors versus learning cycles, (b) smoothing parameters versus learning cycles. Note:  $K_1 = K_{nor} + K_V = 18$ ;  $K_2 = K_1 + K_A = 20$ ;  $K_3 = K_2 + K_L = 27$ ;  $K_4 = K_3 + K_R = 35$ ;  $K_5 = K_4 + K_P = 41$ ;  $K_6 = K_5 + K_F = 43$ .

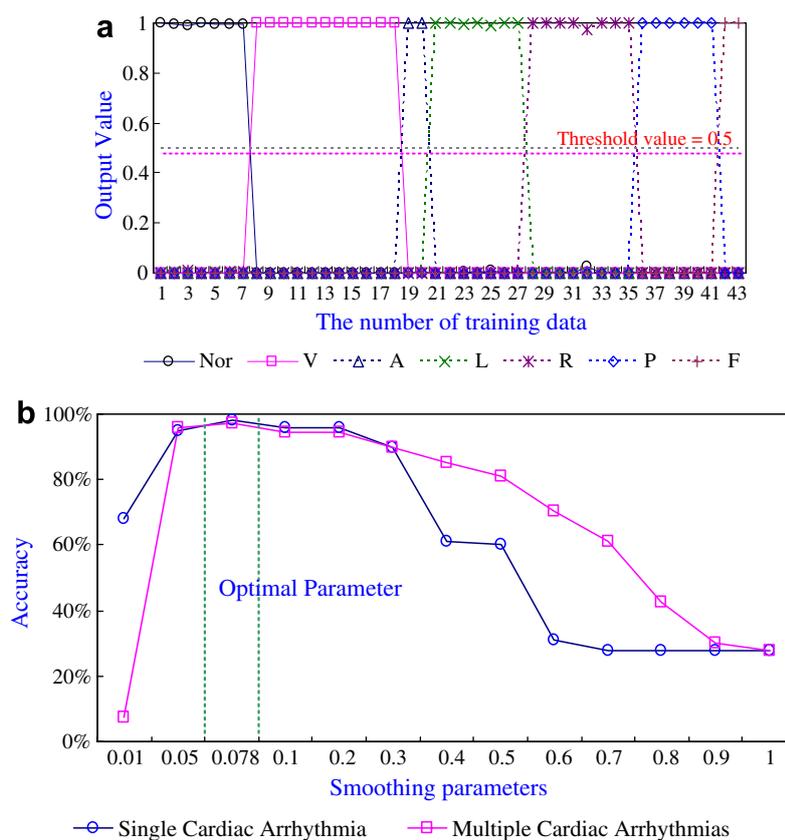


Fig. 9. (a) Output target values of the AWN, (b) detection accuracies versus smoothing parameters.

## 5. Conclusion

The diagnostic procedure based on WT and PNN has been presented to recognize cardiac arrhythmias. For ECG signals, classifier based on AWN is proposed to recognize normal beat, premature ventricular contraction, atrial premature beat, right/left bundle branch block beat, paced beat, and fusion of paced and normal beat. The wavelets act to extract and enhance the features from QRS complexes in the time domain. These features are slightly affected by noise influences. Subsequently, PNN can classify the applied input pattern with/without a noisy background. The AWN model can also work in a dynamic environment with continuity add-in/delete-off features by automatically tuning the targets and smoothing parameters of hidden nodes. For both trained and untrained data, the results demonstrate the efficiency of the proposed method. Compared with the MLNNs, AWN can be built using adaptive training algorithms, and can avoid the determination of network weights by the trial-and-error procedure. Test results show accurate diagnosis, fast learning, good adaptability, and faster processing time for detection. With this model, special features can be further added to the current database such as ventricular bigeminy (*B*), ventricular trigeminy (*V*), ventricular tachycardia (*VT*), normal sinus rhythm (*N*), etc. Thus, the database is always enhancible with new symptomatic patterns. The AWN can adapt itself in a new environment by adding features, and also promise

the high confidence value of detection results with special features considering. The proposed method can be used as an aided tool for heartbeat recognition, and be integrated in the monitoring device.

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