

SP Mean E-Cordial Labeling

¹M. Aishwarya, ^{2*}V. Maheswari and ³V. Balaji

¹Research Scholar, Department of Mathematics, Vels Institute of Science Technology and Advanced Studies, Chennai, Tamil Nadu, India.

Email: aishwaryamuthazhagu@gmail.com

^{2,*}Research Supervisor, Professor, Department of Mathematics, Vels Institute of Science Technology and Advanced Studies, Chennai, Tamil Nadu, India.

Corresponding author: maheswari.sbs@vistas.ac.in

³Associate Professor, Department of Mathematics, Sacred Heart College, Tirupattur, Tamil Nadu, India.

Email: pulibala70@gmail.com

Article History:

Received: 12-11-2024

Revised: 10-12-2024

Accepted: 16-01-2025

Abstract:

Assigning an integer to a vertices or edges is called a vertex or edge labeling respectively. Suppose G is a simple graph. Consider the function f for the edge set $f: R \rightarrow \{0, 1\}$. For each vertex $t \in T$, define $f(t) = \sum f(ut) \setminus ut \in R(G) \pmod{2}$. The function f is known as an E-cordial labeling (E-CL) of G if $|r_f(0) - r_f(1)| \leq 1$, and $|t_f(0) - t_f(1)| \leq 1$ where $r_f(0)$, $r_f(1)$ and $t_f(0)$, $t_f(1)$ are the number of edges and vertices labeled with 0 and labeled by 1 respectively. A graph that admits E-CL is said to be E-cordial graphs (E-CG). Based on the above definition we propose a novel labeling known as SP Mean E-cordial labeling (E-CL). In this paper, we study SP Mean E-CL of several families of graphs such as complete bipartite graphs, complete graphs, wheels, etc.

Keywords: Mean E-cordial labeling, Wheel, Complete graphs

1. Introduction

In this research, a graph is defined as a simple graph G . For graph theory definition and results we refer to F. Harary [1,2]. Rosa [3] introduce a new idea called labeling the graph. Assigning an integer to a vertices or edges is called a vertex or edge labeling respectively. Several labeling introduced by various authors [4,5,6,7,8,9]. Here we discuss with edge labeling.

If a mapping $f: R(G) \rightarrow \{0,1,2 \dots \dots, q\}$ exists, a graph G is said to have elegant edges such that the induced mapping $f^*: T(G) \rightarrow \{0, 1, 2, \dots, p-1\}$ given by $f(u) \leq \sum f(ut) \pmod{|t|}$, $ut \in R(G)$. [10,11,12,13,14,15,16]. The label of vertex v under f is said to be $f(v)$. A mapping $f: T(G) \rightarrow \{0, 1\}$ is known as binary vertex labeling of G .

Cordial labeling is the binary vertex labeling of a graph G if $|r_f(0) - r_f(1)| \leq 1$ and $|t_f(0) - t_f(1)| \leq 1$. A graph satisfies cordial labeling is defined as cordial graph, where $r_f(0)$, $r_f(1)$ and $t_f(0)$, $t_f(1)$ are the number of edges and vertices labeled by 0 and 1 respectively. The cordial labeling introduced in 1987 by Cahit [17].

2. SP Mean E-Cordial Labeling

Definition 2.1 Let G be a simple graph. Let f be a function $f: R \rightarrow \{1,2\}$ and an induced function $f^*: T \rightarrow \{0,1\}$. We associate two integers. $S = \sum f(ut) \setminus ut \in R(G)$ and $P = \prod f(ut)$. For each

vertex u assign the label $\left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$, then f is defined as SP mean E-cordial labeling if $|r_f(1) - r_f(2)| \leq 1$ and $|t_f(0) - t_f(1)| \leq 1$ where $t_f(0)$ and $t_f(1)$ is the number of vertices labeled with 0 and labeled by 1 and $r_f(1)$ and $r_f(2)$ is the number of edges labeled with 1 and labeled by 2 respectively. A graph which admits SP mean E-CL is known as SP Mean E-CG (Figure 1).

Example 2.2

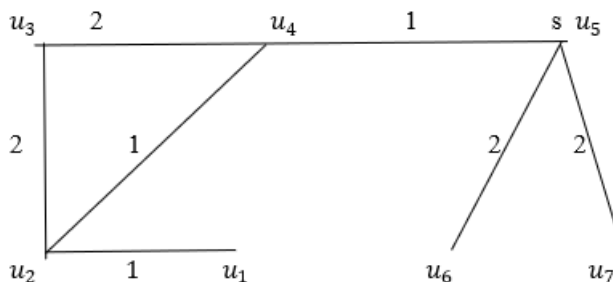


Figure 1. SP Mean E-CG

For vertex u_1 , then $S = 1$ and $P = 1$ then $f^*(u_1) = 1$

For vertex u_2 , then $S = 4$ and $P = 2$ then $f^*(u_2) = 1$

For vertex u_3 , then $S = 4$ and $P = 2$ then $f^*(u_3) = 0$

For vertex u_4 , then $S = 4$ and $P = 2$ then $f^*(u_4) = 1$

For vertex u_5 , then $S = 5$ and $P = 4$ then $f^*(u_5) = 0$

For vertex u_6 , then $S = 2$ and $P = 2$ then $f^*(u_6) = 0$

For vertex u_7 , then $S = 2$ and $P = 2$ then $f^*(u_7) = 0$

Hence $t_f(0) = 4, t_f(1) = 3$ this implies

$$|t_f(0) - t_f(1)| \leq 1$$

Hence the above graph is a SP Mean E-CG.

Theorem 2.3 For any Star $(K_{1,n})$ is SP Mean E-cordial graph if n even.

Proof: Let $T(K_{1,n}) = \{u, u_i / i = 1, 2, \dots, n\}$ be the vertices and $R(K_{1,n}) = \{uu_i / i = 1, 2, \dots, n\}$ be the edges. Then

$$|T(K_{1,n})| = n + 1 \text{ and } |E(K_{1,n})| = n$$

Define the function $f: R(G) \rightarrow \{1, 2\}$ as

$$f(uu_i) = \begin{cases} 2 & \text{if } i \text{ is even} \\ 1 & \text{if } i \text{ is odd} \end{cases}$$

Find $S = \sum f(ut) \setminus ut \in E(G)$ and $P = \prod f(ut)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0, 1\}$ defined by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

Then for $n \equiv 0(mod 4)$

	$t_f(0)$	$t_f(1)$	$r_f(1)$	$r_f(2)$
$n \equiv 0(mod 4)$	$\frac{n}{2}$	$\frac{n}{2} + 1$	$\frac{n}{2}$	$\frac{n}{2}$
$n \equiv 0(mod 4)$	$\frac{n}{2} + 1$	$\frac{n}{2}$	$\frac{n}{2}$	$\frac{n}{2}$

The above labeling satisfies, $|t_f(0) - t_f(1)| \leq 1$ and $|r_f(1) - r_f(2)| \leq 1$.

The Star graph admits SP Mean E-CL.

Hence star graph is a SP Mean E-CG if n is even.

Theorem 2.4 For any Path graph P_n is SP Mean E-CG if n is odd.

Proof: Let $T(P_n) = \{u_1, u_2, \dots, u_n\}$ and $R(P_n) = \{u_1u_2, u_2u_3, u_3u_4, \dots, u_{n-1}u_n\}$ be the vertices and edges respectively. Then $|T(P_n)| = n$ and $|R(K_{1,n})| = n - 1$

Define the labeling function $f: R(G) \rightarrow \{1,2\}$ as follows

$$f(u_iu_{i+1}) = \begin{cases} 1 & \text{if } 1 \leq i \leq \frac{n-1}{2} \\ 2 & \text{if } \frac{n-1}{2} \leq i \leq n-1 \end{cases}$$

Find $S = \sum f(ut) \setminus ut \in R(G)$ and $P = \prod f(ut)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0,1\}$ defined by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

$t_f(0)$	$t_f(1)$	$r_f(1)$	$r_f(2)$
$\frac{n+1}{2}$	$\frac{n}{2}$	$\frac{n-1}{2}$	$\frac{n-1}{2}$

The above labeling satisfies, and $|t_f(0) - t_f(1)| \leq 1$ and $|r_f(1) - r_f(2)| \leq 1$.

The Path graph admits SP Mean E-CL.

Hence Path graph is a SP Mean E-CG.

Theorem 2.5 For any Cycle graph C_n is SP mean E-CG if n is odd.

Proof: Let $T(C_n) = \{u_1, u_2, \dots, u_n\}$ and $R(C_n) = \{u_1u_2, u_2u_3, u_3u_4, \dots, u_{n-1}u_n, u_nu_{n1}\}$ be the vertices and edges respectively. Then $|T(P_n)| = n$ and $|R(K_{1,n})| = n - 1$

Define the labeling function $f: R(G) \rightarrow \{1,2\}$ as follows

$$f(u_i u_{i+1}) = \begin{cases} 1 & \text{if } 1 \leq i \leq \frac{n+1}{2} \\ 2 & \text{if } \frac{n+1}{2} \leq i \leq n-1 \end{cases}$$

Find $S = \sum f(ut) \setminus ut \in R(G)$ and $P = \prod f(ut)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0,1\}$ defined by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

$t_f(0)$	$t_f(1)$	$r_f(1)$	$r_f(2)$
$\frac{n+1}{2}$	$\frac{n-1}{2}$	$\frac{n+1}{2}$	$\frac{n-1}{2}$

The above labeling satisfies, $|t_f(0) - t_f(1)| \leq 1$ and $|r_f(1) - r_f(2)| \leq 1$.

The Cycle graph admits SP Mean E-CL.

Hence Cycle graph is a SP Mean E-cordial graph.

Note 2.6 K_3, K_4 are the only complete graph in SP Mean E-cordial graph.

Theorem 2.7 For any Wheel graph W_n is a SP Mean E-cordial graph if n is even.

Proof: Let $T(W_n) = \{u, u_i \mid i = 1, 2, 3, \dots, n\}$ and $R(W_n) = \{uu_i, u_1u_2, u_2u_3, u_3u_4, \dots, u_nu_1\}$ be the vertices and edges respectively, u is apex vertex and $u_1, u_2, u_3, \dots, u_n$ be the vertices of cycle C_n .

Then $|T(W_n)| = n + 1$ and $|R(W_n)| = n$

Define the labeling $f: R(G) \rightarrow \{1,2\}$ as below

$$f(uu_i) = 2, \text{ if } i \text{ is even}$$

$$f(uu_i) = 1, \text{ if } i \text{ is odd}$$

$$f(u_i u_{i+1}) = 2, \text{ if } i \text{ is even}$$

$$f(u_i u_{i+1}) = 1, \text{ if } i \text{ is odd}$$

Find $S = \sum f(ut) \setminus ut \in E(G)$ and $P = \prod f(ut)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0,1\}$ defined by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

$t_f(0)$	$t_f(1)$	$r_f(1)$	$r_f(2)$
$\frac{n}{2}$	$\frac{n}{2}$	n	n

The above labeling satisfies $|r_f(1) - r_f(2)| \leq 1$ and $|t_f(0) - t_f(1)| \leq 1$.

Hence Wheel graph W_n admits SP Mean E-cordial graph labeling.

Theorem 2.8 For any Bistar $B_{n,n}$ is SP Mean E-CG if n is even.

Proof: Let $T(B_{n,n}) = \{u, t, u_1, u_2, u_3 \dots u_n, t_1, t_2, t_3 \dots, t_n\}$ be the vertices and

$R(B_{n,n}) = \{ut, uu_1, uu_2, uu_3 \dots uu_n, tt_1, tt_2, tt_3 \dots, tt_n\}$ be the edges.

Then $|T(B_{n,n})| = 2n + 2$ and $|R(W_n)| = 2n + 1$

To define the labeling function $f: R(G) \rightarrow \{1,2\}$ as follows

$$f(ut) = 1$$

$$f(ut_i) = 1$$

$$f(tt_i) = 2$$

Find $S = \sum f(ut) \setminus ut \in R(G)$ and $P = \prod f(ut)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0,1\}$ defined by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

$t_f(0)$	$t_f(1)$	$r_f(1)$	$r_f(2)$
$n + 1$	$n + 1$	n	$n + 1$

The above labeling satisfies $|t_f(0) - t_f(1)| \leq 1$ and

$$|r_f(i) - r_f(j)| \leq 1.$$

The Bistar $B_{n,n}$ admits SP Mean E-CL.

Therefore, Bistar $B_{n,n}$ is a SP Mean E-CG.

Theorem* 2.9 Combo graph $P_n \odot K_2$ is a SP Mean E-CG.

Proof: Let $T(P_n \odot K_2) = \{u_i, u'_i | 1 \leq i \leq n\}$ be the vertices and

$R(P_n \odot K_2) = \{u_i u_{i+1}, u u'_i, 1 \leq i \leq n\}$ be the edges.

Then $|T(P_n \odot K_2)| = 2n$ and $|R(P_n \odot K_2)| = 2n - 1$

Define the function $f: R(G) \rightarrow \{1,2\}$ as below

$$f(u_i u_{i+1}) = \begin{cases} 2 & \text{if } i \text{ is even} \\ 1 & \text{if } i \text{ is odd} \end{cases}$$

$$f(u_i u'_i) = \begin{cases} 2 & \text{if } i \text{ is even} \\ 1 & \text{if } i \text{ is odd} \end{cases}$$

Find $S = \sum f(ut) \setminus ut \in E(G)$ and $P = \prod f(ut)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0,1\}$ defined by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

$r_f(1)$	$r_f(2)$	$t_f(0)$	$t_f(1)$
n	n $- 1$	n	n

The above labeling satisfies $|r_f(1) - r_f(2)| \leq 1$ and $|t_f(0) - t_f(1)| \leq 1$.

Combo graph $P_n \odot K_2$ admits SP Mean E-cordial labeling.

Hence Combo graph $P_n \odot K_2$ is a SP Mean E-cordial graph.

Theorem 2.10 Crown graph $C_n \odot K_2$ is a SP Mean E-CG.

Proof: Let $T(C_n \odot K_2) = \{u_1, u_2, u_3 \dots, u_n, u'_1, u'_2, u'_3 \dots, u'_n\}$ be the vertices and $R(C_n \odot K_2) = \{u_1u_2, u_2u_3, u_3u_4, \dots, u_nu_1, u_1u'_1, u_2u'_2, u_3u'_3 \dots, u_nu'_n\}$ be the edges.

Then $|T(C_n \odot K_2)| = 2n$ and $|R(C_n \odot K_2)| = 2n$

Define the labeling function $f: R(G) \rightarrow \{1,2\}$ as below

For $1 \leq i \leq n - 1$

If n is odd

$$f(u_iu_{i+1}) = \begin{cases} 2 & \text{if } i \text{ is even} \\ 1 & \text{if } i \text{ is odd} \end{cases}$$

$$f(u_iu'_i) = \begin{cases} 1 & \text{if } i \text{ is even} \\ 2 & \text{if } i \text{ is odd} \end{cases}$$

If n is even

$$f(u_iu_{i+1}) = \begin{cases} 2 & \text{if } i \text{ is even} \\ 1 & \text{if } i \text{ is odd} \end{cases}$$

$$f(u_iu'_i) = \begin{cases} 2 & \text{if } i \text{ is even} \\ 1 & \text{if } i \text{ is odd} \end{cases}$$

Find $P = \prod f(ut)$ and $S = \sum f(ut) \setminus ut \in E(G)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0,1\}$ by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

	$r_f(1)$	$r_f(2)$	$t_f(0)$	$t_f(1)$
n is even	n	n	n	n
n is odd	n	$n - 1$	n	n

The above labeling satisfies $|r_f(1) - t_f(2)| \leq 1$ and $|t_f(0) - t_f(1)| \leq 1$.

The Crown graph $C_n \odot K_2$ admits SP Mean E-CL.

Hence Crown graph $C_n \odot K_2$ is a SP Mean E-cordial graph.

Theorem 2.11 Triangular snake nC_3 is a SP Mean E-CG.

Proof: Let the path P_n having the edges $r_1, r_2, r_3 \dots \dots, r_{n-1}$ and vertices $t_1, t_2, t_3, \dots, t_n$.

To construct Triangular snake nC_3 from path P_n join u_i and u_{i+1} to a new edge t_i by edges $u_i t_i$ and $u_{i+1} t_i$, for

$$i = 1, 2, 3 \dots \dots, n - 1$$

Then $|T(nC_3)| = 2n - 1$ and $|R(nC_3)| = 3n - 3$

Define the labeling function $f: R(G) \rightarrow \{1, 2\}$

$$f(u_i u_{i+1}) = \begin{cases} 2 & \text{if } i \text{ is even} \\ 1 & \text{if } i \text{ is odd} \end{cases}$$

$$f(u_i u'_i) = 1$$

$$f(u_{i+1} u'_i) = 2$$

Find $S = \sum f(ut) \setminus ut \in E(G)$ and $P = \prod f(uv)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0, 1\}$ defined by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

	$t_f(0)$	$t_f(1)$	$r_f(1)$	$r_f(2)$
n is even	n	$n - 1$	$n + 1$	$n + 1$
n is odd	n	$n - 1$	$n + 1$	$n + 1$

The above labeling satisfies $|r_f(1) - r_f(2)| \leq 1$ and $|t_f(0) - t_f(1)| \leq 1$.

The Triangular snake nC_3 admits SP Mean E-cordial labeling

Hence Triangular snake nC_3 is a SP Mean E-cordial graph.

Theorem 2.12 Fan graph $F_{1,n}$ is a SP mean E-CG if n is odd.

Proof: Let $T(F_{1,n}) = \{u, u_1, u_2, u_3 \dots, u_n\}$ be the vertices and $R(F_{1,n}) = \{u_1 u_2, u_2 u_3, u_3 u_4, \dots, u_{n-1} u_n, uu_1, uu_2 uu_3, \dots, uu_n\}$

be the edges. Here u is apex vertex and $u_1, u_2, u_3 \dots, u_n$ be the vertices of path. Then $|R(F_{1,n})| = 2n - 1$ and $|T(F_{1,n})| = n + 1$.

Define the function $f: R(G) \rightarrow \{1, 2\}$ as below

$$f(uu_i) = \begin{cases} 2 & \text{if } i \text{ is even} \\ 1 & \text{if } i \text{ is odd} \end{cases}$$

$$f(u_i u_{i+1}) = \begin{cases} 1 & \text{if } i \text{ is even} \\ 2 & \text{if } i \text{ is odd} \end{cases}$$

Find $P = \prod f(ut)$ and $S = \sum f(ut) / ut \in E(G)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0,1\}$ by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

$t_f(0)$	$t_f(1)$	$r_f(1)$	$r_f(2)$
$\frac{n+1}{2}$	$\frac{n+1}{2}$	n	$n-1$

The above labeling satisfies $|t_f(0) - t_f(1)| \leq 1$ and $|r_f(1) - r_f(2)| \leq 1$.

The Fan graph $F_{1,n}$ admits SP Mean E-cordial labeling.

Hence Fan graph $F_{1,n}$ is a SP Mean E-CG.

Theorem 2.13 Semi point total graph of path $T_2(P_n)$ is a SP Mean E-CG.

Proof: Let the path P_n having the edges $r_1, r_2, r_3, \dots, r_{n-1}$ and the vertices $u_1, u_2, u_3, \dots, u_n$.

To construct Semi point total graph of path $T_2(P_n)$ from path P_n join u_i and u_{i+1} to a new edge t_i by edges $u_i t_i$ and $u_{i+1} t_i$, for $i = 1, 2, 3, \dots, n-1$.

Then $|T(T_2(P_n))| = 2n - 1$ and $|R(T_2(P_n))| = 3n - 3$

Define the labeling function $f: R(G) \rightarrow \{1,2\}$

$$f(u_i u_{i+1}) = \begin{cases} 2 & \text{if } i \text{ is even} \\ 1 & \text{if } i \text{ is odd} \end{cases}$$

$$f(u_i u'_i) = 1$$

$$f(u_{i+1} u'_i) = 2$$

Find $S = \sum f(ut) \setminus ut \in E(G)$ and $P = \prod f(ut)$ for each vertex in $T(K_{1,n})$

Define $f^*: T(G) \rightarrow \{0,1\}$ defined by $f^*(u) = \left\lfloor \frac{S+P}{2} \right\rfloor \pmod{2}$.

	$r_f(1)$	$r_f(2)$	$t_f(0)$	$t_f(1)$
n is even	$n+1$	$n+1$	n	$n-1$
n is odd	$n+1$	$n+1$	n	$n-1$

The above labeling satisfies $|r_f(1) - r_f(2)| \leq 1$ and $|t_f(0) - t_f(1)| \leq 1$.

The Semi point total graph of path $T_2(P_n)$ admits SP Mean E-CL.

Hence Semi point total graph of path $T_2(P_n)$ is a SP Mean E-CG.

3. Conclusion

In this research, we define a new labeling based on edge is called SP mean E-cordial labeling and SP Mean E-cordial graph. Here is it verified some of the standard graphs like cycle, path, wheel, crown graph, combo graph, Triangular snake graph and Semi point total graph are SP Mean E-cordial graph. In future we extend this work for some more special graphs.

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