

Neural Rewiring: Dynamic Topology Optimization in Deep Architectures

Mrs Beaula Pinky B¹, Assistant Professor

Department of AI&DS, Sri Shanmugha College of Engineering and Technology,
Pullipalayam, Morur (Post), Sankari (Tk), Salem, Tamil Nadu, India

beulapinky@shanmugha.edu.in

Mr. Balaji S², Assistant Professor

Department of Computer Science and Engineering, Sri Shanmugha College of
Engineering and Technology, Pullipalayam, Morur (Post), Sankari (Tk), Salem, Tamil
Nadu, India

balaji.s@shanmugha.edu

Mr. R. Palanivel³, Assistant Professor

Department of Computer Science and Engineering, Sri Shanmugha College of
Engineering and Technology, Pullipalayam, Morur (Post), Sankari (Tk), Salem, Tamil
Nadu, India

palanivel.cs@shanmugha.edu.in

Mr. P. Kameshkumar⁴, Assistant Professor

Department of Computer Science and Engineering, Sri Shanmugha College of
Engineering and Technology, Pullipalayam, Morur (Post), Sankari (Tk), Salem, Tamil
Nadu, India

kameshkumar@shanmugha.edu.in

Abstract- In this research, we propose a deep learning based approach for speeding up the topology optimization methods. The problem we seek to solve is the layout problem. The main novelty of this work is to state the problem as an image segmentation task. We leverage the power of deep learning methods as the efficient pixel-wise image labeling technique to perform the topology optimization. We introduce convolutional encoder-decoder architecture and the overall approach of solving the above-described problem with high performance. The conducted experiments demonstrate the significant acceleration of the optimization process. The proposed approach has excellent generalization properties. We demonstrate the ability of the application of the proposed model to other problems. The successful results, as well as the drawbacks of the current method, are discussed.

Keywords – Deep learning, topology optimization, image segmentation, encoder-decoder architecture.

INTRODUCTION

Topology optimization solves the layout problem with the following formulation: how to distribute the material inside a design domain such that the obtained structure has optimal properties and satisfies the prescribed constraints? The most challenging formulation of the problem requires the solution to be binary, i.e., it should state whether there is a material or a void for each of the parts of the design domain[1]. One of the common examples of such an optimization is the minimization of elastic strain energy of a body for a given total weight and boundary conditions. Initiated by the

demands of automotive and aerospace industry in the 20th century, topology optimization has spread its application to a wide range of other disciplines: e.g. fluids, acoustics, electromagnetics, optics and combinations thereof[2]. All modern approaches for topology optimization used in commercial and academic software are based on finite element methods. SIMP (Simplified Isotropic Material with Penalization), which was introduced in 1989, is currently a widely spread simple and efficient technique[3]. It proposes to use penalization of the intermediate values of density of the material, which improves the convergence of the solution to binary. Topology optimization problem could be solved by using BESO (Bi-directional evolutionary structural optimization) as an alternative[4]. The key idea of this method is to remove the material where the stress is the lowest and add material where the stress is higher. For all of the above-described methods, the process of optimization could be roughly divided into two stages: general redistribution of the material and the refinement. During the first one, the material layout varies a lot from iteration to iteration[5]. While during the second stage the material distribution converges to the final result. The global structure remains unchanged and only local alteration could be observed. In this paper, we propose a deep learning based approach to speeding up the most time-consuming part of a traditional topology optimization methods[6]. The main novelty of this work is to state the problem as an image segmentation task. We leverage the power of deep learning methods as an efficient pixel-wise image labeling technique to accelerate modern topology optimization solvers. The key features of our approach are the following[7]:

- acceleration of optimization process;
- excellent generalization properties;
- absolutely scalable techniques

TOPOLOGY OPTIMIZATION PROBLEM

Current research is devoted to topology optimization of mechanical structures. Consider a design domain $\Omega : \{\omega_j\}_{j=1}^N$, filled with a linear isotropic elastic material and discretized with square finite elements[8]. The material distribution is described by the binary density variable x_j that represents either absence (0) or presence (1) of the material at each point of the design domain. Therefore, the problem, that we seek to solve, can be written in mathematical form as[9]:

$$\begin{cases} \min_{\mathbf{x}} c(\mathbf{u}(\mathbf{x}), \mathbf{x}) = \sum_{j=1}^N E_j(x_j) \mathbf{u}_j^T \mathbf{k}_0 \mathbf{u}_j \\ \text{s.t. } V(\mathbf{x})/V_0 = f_0 \\ \mathbf{K}\mathbf{U} = \mathbf{F} \\ x_j \in \{0; 1\}, \quad j = 1, \dots, N \end{cases}$$

where c is a compliance, \mathbf{u}_j is the element displacement vector, \mathbf{k}_0 is the element stiffness matrix for an element with unit Young's modulus, \mathbf{U} and \mathbf{F} are the global displacement and force vectors, respectively, and \mathbf{K} is the global stiffness matrix; $V(\mathbf{x})$ and V_0 are the material volume and design domain volume, respectively; f_0 is the prescribed volume fraction[10]. The discrete nature of the problem makes it difficult to solve. Therefore, the last constraint in (1.1) is re-placed with the following one: $x_j \in [0; 1], j = 1, \dots, N$ [11]. The most common method for topology optimization problem with continuous design variables is so-called SIMP or power-law approach. This is a gradient-based iterative method with the penalization of non-binary solutions, which is achieved by choosing Young's modulus of a simple but very efficient form[12]:

$$E_j(x_j) = E_{\min} + x_j^p (E_0 - E_{\min})$$

The exact implementation of SIMP algorithm is out of the scope of the current paper. The updating schemes, as well as different heuristics, can be found in excellent papers. The topology optimization code in Matlab is described in the Python implementation of SIMP algorithm is represented in Standard half MBB-Beam problem is used to illustrate the process of topology optimization. The design domain, constraints[13], and loads are represented in Fig. 1. The optimization of this problem is demonstrated in Fig. 2. During the initial iterations, the general redistribution of the material inside of the design domain is performed. The rest of the optimization process includes the filtering of the pixels: the densities with intermediate values converge to binary values and the silhouette of the obtained structure remains almost unchanged[14].

LEARNING TOPOLOGY OPTIMIZATION

As it was illustrated in, it is enough for the solver to perform a few number N_0 of iterations to obtain the preliminary view of a structure. The fraction of non-binary densities could be close to 1, however, the global layout pattern is close to the final one[15]. The obtained image I could be interpreted as a blurred image of a final structure, or an image distorted by other factors. The thing is that there are just two types of objects on this image: the material and the void. The image I^* , obtained as a result of topology optimization does not contain intermediate values and, therefore, could be interpreted as the mask of image I . According to this notation, starting from iteration N_0 the process of optimization $I \rightarrow I^*$ mimics the process of image segmentation for two classes or foreground-background segmentation[16]. We propose the following pipeline for topology optimization: use SIMP method to perform the initial iterations and get the distribution with non-binary densities; use the neural network to perform the segmentation of the obtained image and converge the distribution to $\{0, 1\}$ solution[17].

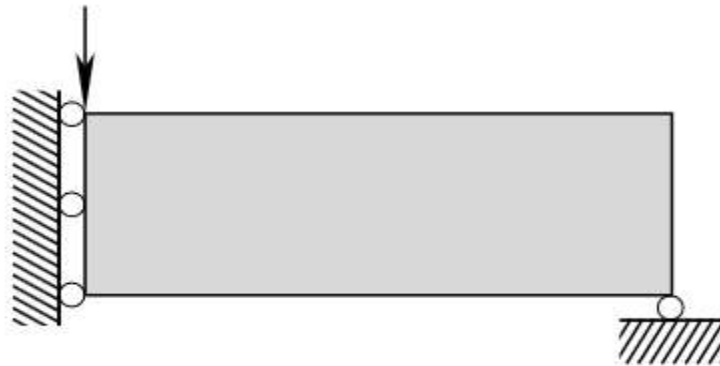


Figure 1- The design domain, boundary conditions, and external load for the optimization of a half MBB beam[4]

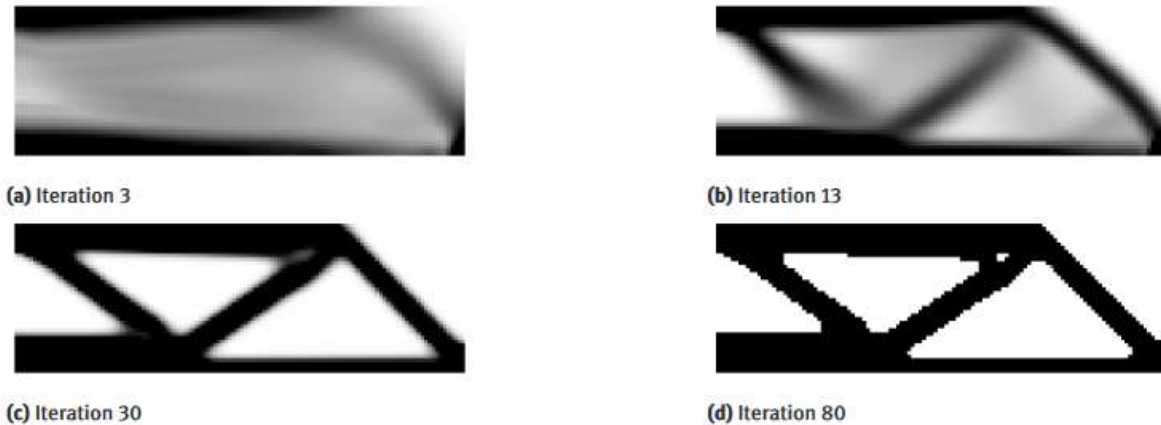


Figure 2- The process of optimization of half MBB beam with SIMP method for 120×40 mesh. Black — 1, white — 0[9]

DEEP ARCHITECTURE

Here we introduce the Neural Network for Topology Optimization deep fully-convolutional neural network aimed to perform the convergence of densities during the topology optimization process. The input of the model is two grayscale images (or a two-channel image). The first one is the density distribution X_n inside of the design domain which was obtained after the last performed iteration of topology optimization solver [18]. The second input is the last performed update (gradient) of the densities $\delta X = X_n - X_{n-1}$, i.e., the difference between the densities after the n th iteration and $(n - 1)$ th iteration. The output of the proposed model is a grayscale image of the same resolution as an input, which represents the predicted final structure [19]. The architecture of our model mimics the common for the image segmentation hourglass shape. The proposed model has an encoder network and a corresponding decoder network, followed by a final pixel-wise classification layer. The architecture is illustrated in Fig. 3. The encoder network consists of 6 convolutional layers. Each layer has kernels of size 3×3 and is followed by ReLU nonlinearity [20]. The first two layers have 16 convolutional kernels. This block is followed by the pooling of the maximal element from the window of size 2×2 . The next two layers have 32 kernels and are also followed by MaxPooling layer. The last block consists of 2 layers with 64 kernels each. The decoder network copies the architecture of the encoder part and reverses it. The MaxPooling layers are replaced with Upsampling layers followed by the concatenation with features from the corresponding low-level layer as it is performed in U-Net [21-27]. The pooling operation introduces the invariance of the subsequent network to small translations of the input. The concatenation of features from different layers allows one to benefit from the use of both the raw low-level representation and significantly encoded parameterization from the higher levels. The decoder is followed by the Convolutional layer with 1 kernel and sigmoid activation function. We included 2 Dropout layers as the regularization for our network [22-27].

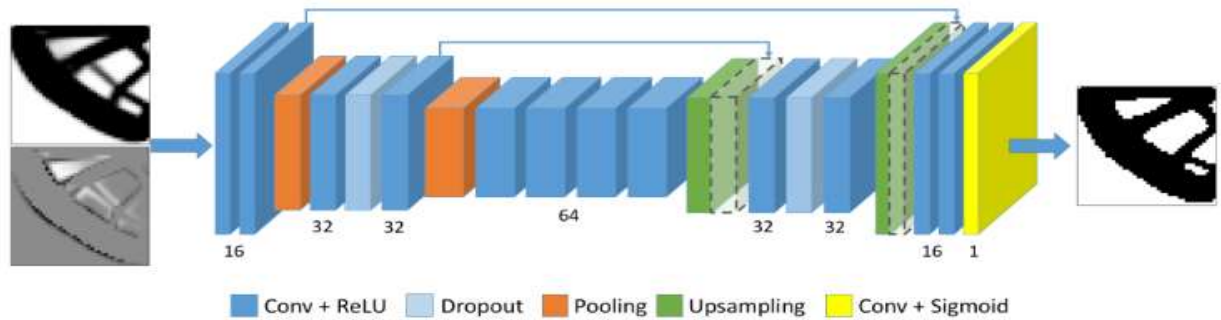
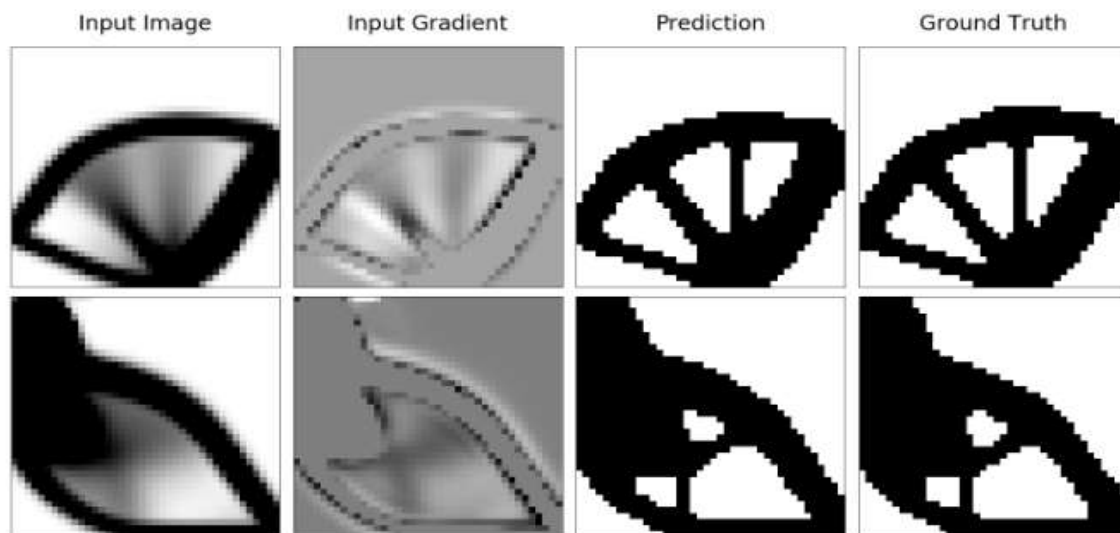


Figure 3- The architecture of the proposed neural network for topology optimization[11]

ACCURACY AND PERFORMANCE

We conducted several experiments to illustrate the results of the application of the proposed pipeline and the exact model to mechanical problems. Figure 4 demonstrates that our neural network restores the final structure while being used even after 5 iterations. The output of the model is close to that of SIMP algorithm. The overall topology of the structure is the same. Furthermore, the time consumption of the proposed method, in this case, is almost 20 times smaller. Neural networks trained with different policies produce close results: models preserve the final structure up to some rare pixel-wise changes[21]. However, the accuracy of these models depends on the number of the initial iterations performed by SIMP algorithm. Tables 1 and 2 summarize the results obtained in the series of experiments. The trained models demonstrate the sufficiently more accurate results comparing to the thresholding applied after the same number of iterations of SIMP method. Some models benefit when they are applied after 5-10 iterations, while others demonstrate better result in the middle or at the end of the process. The proposed pipeline could significantly accelerate the overall algorithm with minimal reduction in accuracy, especially when CNN is used at the beginning of the optimization process[22].



**Figure 4- Top: SIMP is stopped after 8 iterations, binary accuracy 0.96, mean IoU 0.92;
Bottom: solver is stopped after 5 iterations, binary accuracy 0.98, mean IoU 0.95[2]**

CONCLUSION

In this paper, we proposed a neural network as an effective tool for the acceleration of topology optimization process. Our model learned the mapping from the intermediate result of the iterative method to the final structure of the design domain. It allowed us to stop SIMP method earlier and significantly decrease the total time consumption. We demonstrated that the model trained on the dataset of minimal compliance problems could produce the rough approximation of the solution for other types of topology optimization problems. Various experiments have shown that the proposed neural network transfers successfully from the dataset with a small resolution to the problems defined on the grids with better resolution.

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