Chaotic Oscillationofa Three-bus Power System Model Using ElmanNeural Network

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Abstrak

Paper ini meneliti dan membahas secara mendalam mengenai osilasi *chaotic* pada sistem tenaga listrik.Dengan menggunakan sebuah *three-bus* pada sistem tenaga listrik, rute mungkin menyebabkan unjuk kerja *chaotic* sehingga dievaluasi, digambarkan serta dibahas dalam penelitian ini. Osilasi *chaotic* ini dimodelkan menggunakan *Elmanneural network* karena bentuknya yang sederhana dan juga melibatkan algoritma*backpropagation* dengan *adaptive learning rate* dan momentumnya.Unjuk kerja *learning rate* dan momentumnya lebih baik dibandingkan jika tanpa momentumnya. Unjuk kerja *chaotic* dalam sistem tenaga listrik muncul karena sistem ini dioperasikan dalam mode *critical*. Unjuk kerja *chaotic* ini terdeteksi dengan munculnya sebuah*chaotic attractor*dalam *phase-plane trajectory*.

Kata kunci:sistem tenaga listrik, Elman neural network, chaotic attractor, phase-plane trajectory

Abstract

Chaotic oscillation of power systems was deeply studied in this paper. By using a three-bus power system, route may cause chaotic behavior in power systems are evaluated, illustrated and discussed. Chaotic oscillation power systems was modeled using Elman neural network because the Elman neural networkhas a simple form. Backpropagation algorithm with adaptive learning rate and momentum was proposed in this research. Performance of learning rate with momentum was better than learning rate without momentum. Chaotic behaviors in a power systems was detected by appearing a strange attractor (a chaotic attractor) in phase-plane trajectory.

Keywords: power systems, Elman neural network, chaotic attractor, phase-plane trajectory

1. Introduction

In recent years, electric power consuming has grown up rapidly. On the other hand, the power plants and transmission systems being built are very slow due to environmentaland economical constraints. This condition will make the power systems operate in critical mode at the boundary of stability region. Meanwhile, chaotic phenomena is one type of un-deterministic oscillations exist in deterministic systems such as in power system model. Chiang et al, have builtvoltage collapse model, both physical explanations and computational considerations of this model are presented. Static and dynamic models are used to explain the type of voltage collapse, where the static is used before a saddle-node bifurcation and the dynamic model is employed after the bifurcation [1]. Lyapunov exponent, measuring how rapidly two nearby trajectories separate from one another within state space and broad-band spectrum was used to confirm the observation [2]. Within the range of loading conditions, the sensitive dependence feature of chaotic behaviors makes the power system unpredictable after a finite time. In addition, within the range the effectiveness any control scheme was questionable and should bere-evaluated based on state vector information.Furthermore,nonlinear phenomena including bifurcation, chaos and voltage collapse occurred in a power system model. The present of the various nonlinear phenomena was found to be a crucial factor in the inception of voltage collapse in this

model. The problem of controlled and suppressed of the presence of non-linear phenomena in power systems were addressed here in this paper. The bifurcation control approach is approach to modify the bifurcations and to suppress chaos [3,4]. The presence of chaos in a power system causing seriously unstable problem was studiedby Yu, et al.[5]. The existence chaos in power systems due to disturbing of energy at rotor speed has been found in Ref.[6]. One scheme of chaos utility was used on electrical systems for smelting which was based on chaos control. Lei et al. Demonstrated that chaotic steel-smelting ovens regulate their heating current according to chaos control theory [7]. A control system using a neural network controller was presumed to be able to stabilize the unstable focus points of 2-dimensional chaotic systems; although, Konishiand Kokame stated that the control system did not require this presumption [8]. Elman neural network was used to predict short-term load forecasting in power systems [9]. Modeling of chaotic behavior using RNN has been studied in [10]. Various studies on controlling transient chaos have been carried out, such as those by Dhamala et al., and Dhamala and Lai attempted to control transient chaos in power systems using a data time series [11,12]. Strategies for controlling chaos in process plants have been tested on the Henon mapdiscrete chaotic system [13].

In this paper, we focused on the cause of chaotic oscillation in power systems and its model. By using Elman neural network model is proposed. The reason of using the Elman neural network because the Elman network is able to traindata both on present input and on past output, and other reason because an Elman RNN has simple form.

This paper is organized as follows: in advance, power system model used in this research is given in Section 2. Then, Elman neural network model is explained in Section 3. Chaotic behavior due to sensitivity of initial condition and analysis a chaotic behavior are presented in Section 4 and 5, respectively. The conclusionis given in the last section.

2. Power System Model

A Synchronous machine was modeled as a voltage (E_{q0}) behind a direct reactance (x_d). The voltage magnitude was assumed as remaining constant at the pre-disturbance value, as shown in Fig.1(a).De Mello and Concordia as well as Padiyar and Kundur derived of a machine connected toan infinite bus [13,14]. Meanwhile, if saturation and the stator resistance were neglected, the system condition was balanced with a static load. The mechanical mode block diagram of single-machine connected to infinite bus is shown in Fig.1(b).



Figure 1.Single machine connected to infinite bus.

(a) Circuit equivalent (b)Mechanical mode.

The machine wasconnected to infinite bus and supplied the load. Then the armature current flowedfrom the machine to the load. This current causedelectrical torque on the stator winding, and vice versa. The mechanical torque was produced by flux through the rotor winding. Meanwhile, whenthe rotor speed wasconstant, the rotor speed followed thesynchronous speed. When there was imbalanced energy, the rotor speed accelerated or decelerated and caused the swing equation. The swing equation is represented as follows:

$$H\ddot{\delta} + D\,\Delta\omega = T_a = T_m - T_e \tag{1}$$

Where D, $\Delta \omega$ are amping constant and rotor speed deviation, respectively. Eq.1 is a basic equation for mechanical modeof single machine connected to infinite bus. Furthermore, the the Eq. 1 can be expressed as follows:

$$\dot{\delta} = \omega_B \Delta \omega \tag{2}$$
$$\Delta \dot{\omega} = \frac{1}{M} \left(\Delta T_m - \Delta T_e - D \Delta \omega \right) \tag{3}$$

Where ΔT_m , ΔT_e , δ , $\Delta \omega$, *D* and *M* are mechanical torque, electrical torque, power angle, speed rotor, damping constant, inertia constant respectively. The system was developed from Ref.[3] and shown in Fig.3, which is regarded as one synchronous machine supplying power to a local dynamic load shunt with a capacitor (Bus 2) and connected by weak tie line to the extern system (Bus 3). The system equations are:

$$\delta = \Delta \omega .$$

$$\Delta \dot{\omega} = 16.667 \sin (\delta_L - \delta + 0.087) V_L \qquad (5)$$

$$-3.333.d.\Delta \omega + 1.881 \qquad (5)$$

$$\dot{\delta}_L = 496.872 V_L^2 - (6) - 166.667 \cos (\delta_L - \delta - 0.087) V_L - 93.333 V_L \qquad (6) - 666.667 \cos (\delta_L - 0.209) V_L - 33.333 Q_{1d} + 43.333$$

$$\dot{V}_L = -78.764 V_L^2 + 26.217 \cos (\delta_L - \delta - 0.012) V_L + 14.523 V_L + 104.869 \cos (\delta_L - 0.135) - 5.229 Q_{1d} - 7.033$$

Table 1. Power system parameters							
Y ₀	Ym	θ_0	θ_m	V ₀	Vm	P_m	М
20.	5.0	-5.	-5.	1.0	1.0	1.0	0.3
0		0	0				
D	Τ	С	K _{pω}	K _{pv}	$K_{q\omega}$	K_{qv}	K _{qv2}
0.0	8.5	12.	0.4	0.3	-0.0	-2.	2.1
5		0			3	8	

(4)



Figure 2.One line diagram power system with 3 buses.

 $\delta_{L} \Delta \omega_{L} d_{L} Q_{Id}, \delta_{L}, V_{L}$, are the power angle, rotor speed deviation, damping constant, reactive load, voltage angle and magnitude at load bus, respectively. Eqs.4,5,6,and7 can be simplified into a uniform equation in Eq.8.

$$\dot{x} = f(x, \lambda), \quad x \in \mathbb{R}^n, \lambda \in \mathbb{R}^p$$
, (8)

Where *x* is vector state variables and λ is vector of parameters. The state variables are $x = [\delta_{\lambda} \Delta \omega, \delta_{L}, V_{L}]^{T}$, superscript *T* denote transpose of the associate vector.

3. ElmanNeural Network Model

Recurrent Elman network commonly is a two-layer network with feedback from the first-layer output to the first-layer input. This recurrent connection allows the Elman network to both detect and generate time-varying patterns. A two-layer Elman network is shown in Fig.3. The Elman network has tansig neurons in its hidden (recurrent) layer and purelin in its output layer. The Elman network differs fromconventional two-layer networks in that the first layer has a recurrent connection. The delay in this connection stores values from the previous time step, which can be used in the current time step. Thus, even if two Elman networks with the same weight and bias, are given identical inputs at a given time step, their outputs can be different due to different feedback states. Because network can store information for future reference, it is able to learn temporal pattern as well as spatial patterns [15,16,17,18]. The Elman network can be trained to respond and to generate, both kinds of patterns.

$$\frac{a^{1}(n) = \operatorname{tansig}[IW_{1,1} p + LW_{1,1}a^{1}(n-1) + b_{1}]}{a^{2}(n) = purelin[LW_{2,1}a^{1}(n) + b_{2}]}.$$
(9)

The architecture 4:8:8:4 RNN is used in this research. Where $p_{a}(n)$, $a^{2}(n)$, $IW_{1,1}$, $LW_{1,2}$, b_{1} and b_{2} are the vector input, recurrent-layer output, purelin-layer output, weight first-layer, weight hidden layer back to first-layer, weight hidden layer to output layer and biases, respectively.



Figure 3.Elman recurrent neural network block diagram[18]

The RNN wastrained by using 1000 data points. Tansig and purelin activation function were used at hidden layer and at output layer, respectively. Data time series were obtained from the mathematical (exact) model in Eqs.4-7, respectively. The network performance is measured by mean square error (MSE). Formula of the MSE can be expressed by equation as follow:

$$MSE = \frac{1}{k} \left[\sum_{i=1}^{k} (\hat{x}_{i} - x_{i})^{2} \right]$$
(10)

Where k, x_n and \hat{x}_n are the size of data, input and estimation n^{th} data.

4. Chaotic Behavior due to Sensitivity of InitialCondition

Chaos definition and its properties have been given by Devaney and Alligood et al.[19,20]. Sensitivity of initial condition is one type of chaos properties. It is described by existing route to chaotic behavior in power systems caused by sensitivity of initial condition rotor speed (ω_0). Initial rotor speed (ω_0) in power systems was presented by disturbing of energy (DE). Kinetic energy disturbance was related to rotor speed deviation only. The large rotor speeddeviation was implemented as a large DE. When DE was smaller than the value of 1.3824 rad/s ($\omega_0 < 1.3824$ rad/s) a power system converged to a stable equilibrium point. When the DE was increased, the convergencebecame more difficult. At $\omega_0 = 1.3825$ rad/s, power systems produced route to a chaotic behavior in a longer time. When the DE was from 1.3825 to 17003 rad/s, the final states were controlled by a chaotic behavior. Furthermore, while the DE excess than 1.7004 rad/s the system went to divergence or voltage collapse. Based on the simulation result it is shown that chaotic behavior in power systems due to disturbing of energy at the rotor speed deviation.

Table 2. System condition with different initial rotor speed (ω_0)

$\omega_0(rad/s)$	Times (s)	Final state	Time response
0.5	1000	Equilibrium point	Fig.4(a)
1.3824	1000	Equilibrium point	Fig.4(b)
1.3825	1000	Chaotic	Fig.5(a)
1.7003	1000	Chaotic	Fig.5(b)
1.7004	10	Divergen	-



Figure 4.Simulation results with equilibrium point state



Figure 5.Simulation results with chaotic state



Figure 6. (a).Chaotic behavior of the rotor speed deviation (b). Magnified of Fig. 5 from time = 0 to time = 50 s

5. Result and Analysis

In this research, RNN initial simulation parameters were taken: learning rate train parameter = 0.17; increment learning rate = 1.2; decrement learning rate = 0.6; and momentum learning rate = 0.75. The training performance of RNN using adaptive learning rate and adaptive learning rate with momentum are listed in Table 3. The training process is organized as follows: performances (MSE) are obtained to 14.7001×10^{-4} and 4.2209×10^{-4} at disturbance $\omega_0 = 0.5$ rad/s for algorithm backpropagation adaptive learning rate (traingda) and backpropagation learning rate algorithm with momentum (traingdx), respectively. Moreover, performances were obtained to 16.8361×10^{-4} and 4.6115×10^{-4} at disturbance ω_0 1.3825 rad/s. Furthermore, performances were obtained to 17.4185×10^{-4} and 4.9442×10^{-4} at the disturbance ω_0 at the value of 1.7003 rad/s. During the training process the best performancewas obtained to 4.2209×10^{-4} at the disturbance of 0.5 rad/s.



Figure 7. The chaotic behavior of the $\Delta \omega$ at $\omega_0 = 1.7003$ rad/s (a). Blue = exact model; red = RNN model (b). Error signal of the $\Delta \omega$

Figs.7-9 show the time responses of an exact and Elman recurrent neural network (RNN) model. Fig.7(a) shows rotor speed deviation ($\Delta \omega$) time response which was oscillated due to the disturbance occurred at ω_0 1.7003 rad/s. Rotor speed oscillations exist in range from -1.6052 to 1.5679 rad/s and from -1.511 to 1.6045 for the exact and RNN, respectively. Fig. 7(b) shows error signal of the rotor speed deviation; where the error signal is the difference of the exact and RNN model of the rotor speed deviation.

Voltage angle (δ_L) at Bus 2 is affected by disturbing of energy (DE) at generator bus ($\omega_0 0.5$ rad/s). The oscillation on voltage angle occurred at generator bus in a few second, then this oscillation decreased gradually and route to equilibrium point (fixed point) at point of 0.1128and 0.1116 rad for exact and RNN models, respectively. The error signal of the voltage angle was measured by mean square error (MSE = 3.8193%), and these results are shown in Table 4.



Figure 8.The chaotic behavior of the voltage angle when ω_0 at 1.7003 rad/s. (a). Blue = exact; red = RNN (b). Error signal of the δ_L



Figure 9. The voltage magnitude (V_L) time response at $\omega_0 = 1.7003$ rad/s (a). Blue = exact model; red = RNN model (b). Error signal of the V_L

The voltage angle oscillation increased at the disturbance 1.3825, 1.600 and 1.7003 rad/s for exact model with amplitude in ranges (0.0600 to 0.1995 rad), (0.0351 to 0.2730rad), (0.0345 to 0.2748rad) and (0.0340 to 0.2756rad), respectively. And the oscillation for RNN model arefrom 0.0501 to 0.1879 rad, from 0.0460 to 0.2644rad, from 0.0332 to 0.2618radand from 0.0342 to 0.2613rad, respectively. This oscillation occurred in a longer time. Voltage angle time response occurring at disturbance ω_0 1.7003 rad/s can be shown in Fig. 8.

When the disturbance (ω_0) at the value of 0.5 rad/s,the voltage magnitude oscillated in a few seconds. Furthermore, its decreased gradually route to equilibrium state (fixed point) at point 1.095 pu and 1.008 for exact and RNN model, respectively. By increasing disturbance at ω_0 1.3824 rad/s voltage magnitude is oscillated in a longer time in ranges (0.9967 to 1.1207pu) and then amplitude reduced and fixed point at 1.1095 pu (1520 s).

On the opposite, when the disturbing of energy was increased up to 1.3825, 1.600 and 1.7003 rad/s, voltage magnitude oscillated for the exact model where the amplitude increased from 0.8307 to 1.1220pu, from 0.8285 to 1.1118puand from 0.8290 to 1.1119pu, respectively. And the oscillation for RNN model was in the ranges from 0.8497 to 1.1158pu, from 0.8580 to 1.1235puand from 0.8642 to 1.1185pu, respectively. In Fig.9, we can show that the voltage magnitude of the exact and RNN modelsexhibit chaotic behavior.

		<u> </u>	V	U	
ω ₀	Training	Times (s)	Performances MSE (×10 ⁻⁴)		
(rad/s)	×1	1 0 ²			
	traingda	traingdx	traingda	traingdx	
0.5	69.3861	37.403	14.7001	4.2209	
1.3824	68.3250	42.342	17.2014	4.9080	
1.3825	67.3329	36.750	16.8361	4.6115	
1.7003	70.5781	41.840	17.4185	4.9442	

Table 3.Performance of training algorithm using learningrate momentum

State trajectory(orbit) of the $\Delta\omega$ against δ s shown in Fig.10, where many circlesare made by themselves with boundary ranges from -1.6011 to +1.5535 rad/sandfrom -0.1165 to +0.7583 rad for the ω_{min} - ω_{max} and δ_{min} - δ_{max} , respectively. Thestate trajectoriesofthe RNN model are made in rangesfrom -1.6020 to +1.5524 rad/sandfrom -0.1145 to +0.7598 rad, respectively. The attractive form of the $\Delta\omega$ - δ s known as strange attractor (chaotic attractor). The strange attractorsof the δ_L against V_L are shown in Fig.11. The strange attractor coordinateswere from 0.0345to 0.2748 rad and from 0.8285 to 1.1118pu for δ_{Lmax} - δ_{Lmain} and V_{Lmax} - V_{Lmin} , respectively.

Meanwhile, the RNN model of the δ_L - V_L was from 0.0332to 0.2618 rad and from 0.8280 to 1.1235pu for δ_{Lmax} - δ_{Lmin} and V_{Lmax} - V_{Lmin} , respectively.

Table4.Power system state when variation of the DE was applied.					
<i>w</i> ₀&Model	<i>δ</i> (rad)	<i>ω</i> (rad/s)	δ_L (rad/s)	<i>V</i> ∠ (pu)	
0.5Exact	eq 0.3095	osc-0.2104 to	eq	eq 1.095	
		0.2123	0.1128		
RNN	eq 0.3194	osc-0.2008 to	eq	eq 1.008	
		0.2010	0.1116		
MSE (%)	0.2636	11.1792	3.8193	8.7051	
1.3824Exact	osc-0.0245	osc-1.1546 to	osc0.0600 to	osc0.9967 to	
	to 0.6160	1.1049	0.1995	1.1207	
RNN	osc-0.0256	osc-1.0246 to	osc0.0501 to	osc0.9970 to	
	to 0.6165	1.0049	0.1879	1.1135	
MSE (%)	3.9625	6.3023	0.2040	0.1154	
1.3425Exact	osc-0.1156	osc-1.5711 to	osc0.0351 to	osc0.8307 to	
	to 0.7578	1.5142	0.2730	1.1220	
RNN	osc-0.1148	osc-1.5734 to	osc0.0460 to	osc0.8497 to	
	to 0.7510	1.5165	0.2644	1.1158	
MSE (%)	0.68	0.23	1.09	1.90	
1.6000Exact	osc-0.1165	osc-1.6011 to	osc 0. 0345	osc 0.8285 to	
	to 0.7583	1.5535	to 0. 2748	1. 1118	
RNN	osc-0.1645	osc-1.6020 to	osc0.0332 to	osc0.8580 to	
	to 0.7598	1.5524	0. 2618	1. 1235	
MSE(%)	0.2163	2.8779	0.0460	0.0407	
1.7003Exact	osc1157 to	osc-1.6052 to	osc 0. 0340	osc 0.8290 to	
	0.7601	1.5679	to 0. 2756	1. 1119	
RNN	osc-0.1345	osc-1.511 to	osc 0.0342 to	osc 0.8642 to	
	to 0.7457	1.6045	0. 2613	1. 1185	
MSE(%)	1.0522	17.8296	0.1284	0.1470	

Note: eq = equilibrium point (fixed point); osc = oscillation.



Figure 10. State trajectory of the $\Delta \omega$ - δ when disturbance was applied at $\omega_0 = 1.600$ rad/s

Furthermore, existence of the chaotic attractors can also be depicted in Figs.12 and 13 for the $\omega_0 1.7003$ rad/s. Fig.12 was produced by the $\Delta \omega$ againsts δ state trajectories at coordinates from -1.6052 to +1.5679 rad/sandfrom -0.1157 to +0.7601 rad for the ω_{min} - ω_{max} and δ_{min} - δ_{max} , respectively. The results of theRNN model are depicted by red circles at coordinates from -1.5110 to +1.6045 rad/sandfrom -0.1345 to +0.7457 rad for the ω_{min} - ω_{max} and δ_{min} - δ_{max} , respectively.

Fig.13 shows the δ_L against V_L state trajectories at coordinates from 0.0351to 0.2756 rad and from 0.8290 to 1.1119 pu for the δ_{Lmax} - δ_{Lmin} and the V_{Lmax} - V_{Lmin} , respectively. State trajectories of the RNN model can be depicted by red points at coordinates from 0.0342to 0.2613 rad and from 0.8642 to 1.1185 pu for the δ_{Lmax} - δ_{Lmin} and the V_{Lmax} - V_{Lmin} , respectively. The complete simulation results are tabulated in Table 4.



Figure 11. The δ_L -V_L state trajectory when the DE at ω_0 = 1.6 rad/s was applied



Figure 12. The $\Delta \omega$ - δ state trajectory when the DE at the value of 1.7003 rad/s was applied to a power system



Figure 13. The δ_L - V_L state trajectory when the DE at the value of 1.7003 rad/s was applied to a power system

Based on the in Table4that the largest MSE was 17.8296, where the largest MSE was obtained on the speed rotor deviation ($\Delta \omega$) at the value of 1.7003 rad/s. Simulation results show that chaotic behavior of power systems can be modeled by the Elman recurrent neural network.

6. Conclusion

Chaotic oscillations power systems using exact and RNN models are deeply studied in this research. The exact model was obtained using mathematical model. Then, the RNN model is obtained by training process using the data from exact model simulation. The training of the RNN model using adaptive learning rate both with and without momentum is compared. The performace of the adaptive learning rate with momentum is better than the other one. Chaotic behaviors are detected in power systems by appearing chaotic attractors both at power angle-rotor speed and at magnitude-angle voltage state trajectories in phase-plane.

7. Future Works

Chaotic behavior of power systems was an interest topic research in recent years. In the future, thechaotic behavior of power systems should be reduced and vanished by applying control strategy properly.

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