

# Zagreb Topological indices for hexadentate 3hydroxypyridinones-terminated dendrimers used in iron binding and anti-microbial activities

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**Abstract.** Among the degree based topological indices which are mostly used in the study of chemical graph theory, the Zagreb index plays a prominent role in the study of therapies and treatments. There were different versions of the Zagreb indices defined in the literature and used for different purposes. In this paper, we calculated the different versions of the Zagreb indices for the hexadentate 3-hydroxypyridinones-terminated dendrimers which are used in iron binding and anti-microbial activities. These indices may play an important role in determining properties of these compounds.

**Keywords:** Anti-microbial activities, dendrimers, iron binding, topological index, Zagreb index.

# 1 Introduction

Iron performs a crucial role in the growth and development of living systems. Therefore, it is one of the most vital trace elements in biological systems (Weizman *et al.* 1996). Iron is an essential element in hemoglobin, myoglobin, cytochromes and important in many biological processes (Haas and Browlie 2001, Zhang and Enns 2008, Evstatiev *et al.* 2012). However, both iron deficiency and the excessive iron in the body are harmful to human health. Excessive iron in the body is usually removed by iron-specific chelators (Saliba *et al.* 2016). Of the few iron specific chelators, macromolecular iron chelators play a major role in the treatment in removing both chronic and acute excessive iron in the body (Mahoney *et al.* 1989). Dendrimers are a class of synthetic macromolecules with highly branched structures which built up by repeating the assembly of the constituent layers or generations. These structures have a central core and different functional groups attached to their outer surface (Zhu and Shi 2013). These dendrimer structures are used as iron chelators for therapeutic purposes. These iron chelators bind to the iron and to the complex which are kinetically inert and non-toxic. Furthermore, these complexes are not absorbed by the



gastrointestinal tract of the human due to their large size so will be excreted from the human body. Furthermore, the macromolecular iron chelators inhibit the growth of bacteria hence are used in the treatment of wound healings (Zhou *et al.* 2011). Zhou et. al synthesized hexadentate 3-hydroxypyridinones-terminated dendrimers that could be used for iron bindings and anti-bacterial purposes (Zhou *et al.* 2018).

Chemical graph theory is an important tool for studying molecular structures. In theoretical chemistry, molecular descriptors, especially topological indices are used for modelling information of molecules which are used in biology and pharmacology. Therefore, determining topological indices of dendrimers will give a suitable correlation between chemical structure and its activity (Farahani *et al.* 2015, Soleimani *et al.* 2016). In this work, different versions of the Zagreb indices are calculated for the hexadentate 3-hydroxypyridinones-terminated dendrimers which are used in iron binding and anti-microbial activities.

A molecular graph is a simple graph which has neither loops nor multiple edges. The atoms and the chemical bonds between them in molecular graphs, are represented by vertices and edges respectively in the graph theory. A graph G = G(V, E) is a pair of nonempty set of vertices V = V(G) and the set of connected edges E = E(G) if there exists a connection between any pair of vertices in G. The degree  $d_v(G)$  or  $d_v$  of a vertex v in the set of vertices V(G) in a connected graph G is the number of vertices which are connected to that vertex by the edges. The concept of degree is closely related to the concept of valence bond in chemistry (Gutman 2013).

A topological index is a numerical quantity which is derived mathematically in a direct and unambiguous manner from the structural graph of a molecule. The topological index is defined to be a function Top:  $G(V, E) \rightarrow R$ , where *R* is the set of real numbers. If two graphs are isomorphic then their topological indices are same. Many properties of a chemical compound are closely related to some of the topological indices of its molecular graph. The Wiener index is the first and the most studied distance-based topological index in chemical graph theory. This index was introduced by the chemist H. Wiener (Wiener 1947) in 1947 to demonstrate the correlations between physicochemical properties of organic compounds and the topological structure of their molecular graphs. The Wiener index was defined as the sum of distances between all the carbon atoms in the molecules, in terms of carbon-carbon bonds.

Among the different types of topological indices, the degree-based topological indices are the mostly studied type of topological indices, which play a prominent role in chemical graph theory. One of the oldest degree-based topological indices is the well-known Zagreb index which was introduced by Gutman and Trinajstić (1972) during the analysis of the structure-dependency of total  $\pi$ -electron energy. Currently researchers are interested in calculating the Zagreb indices for different types of molecular structures which are used in various applications (Aslam *et al.* 2017, Kana *et al.* 2018, Jude *et al.* 2019).

#### 2 Methods

In this paper we considered four types of the hexadentate 3-hydroxypyridinonesterminated dendrimers which are used in iron binding and anti-microbial activities. Zhou *et al.* 2018 shows that the convergent synthesis of a range of novel hexadentate 3-hydroxypyridinone-terminated dendrimers. Initially, first generation dendrimeric chelators were synthesized and as its structure shown in Figure 1 which contain three hexadentate moieties. The second generation of this dendrimeric chelators was synthesised by the same authors and its structure is shown in Figure 2. Second generation dendrimer was respectively conjugated with di-acid and tri-acid to form protected structures in Figure 3 and Figure 4 which contain six and nine hexadentate centres respectively. We calculated four different versions of the Zagreb indices using the following formulas.

The first Zagreb index (Gutman and Trinajstić 1972) was defined as

$$M_1(G) = \sum_{v \in V(G)} (d_v)^2 = \sum_{uv \in E(G)} (d_u + d_v)$$

and the second Zagreb index (Gutman and Trinajstić 1972) was defined as

$$M_2(G) = \sum_{uv \in E(G)} d_u d_v$$

The second modified Zagreb index (Hao 2011) was defined as

$${}^{m}M_{2}(G) = \sum_{uv \in E(G)} \frac{1}{d_{u}d_{v}}$$

The reduced second Zagreb index which appeared in the literature earlier but so far not been studied in mathematical chemistry was re-presented in the paper (Gutman *et al.* 2015) with its main mathematical properties. This was defined as

$$\mathrm{RM}_{2}(\mathrm{G}) = \sum_{\mathrm{uv} \in \mathrm{E}(\mathrm{G})} (\mathrm{d}_{\mathrm{u}} - 1)(\mathrm{d}_{\mathrm{v}} - 1)$$

This is of the difference between the two Zagreb indices  $M_1(G)$  and  $M_2(G)$  and if the graph G is a tree, then this is equal to the number of pairs of vertices at distance 3, which is often referred to as the "Wiener polarity index" in mathematical chemistry (Gutman *et al.* 2014).

# **3** Results and Discussion

By observing the structure of synthetic route of the first generation dendrimeric chelators, we inferred six partitions of the edge set as:

$$\begin{split} E_1(G) &= \{e = uv \in E(G) : d_u = 1 \text{ and } d_v = 2\}, \\ E_2(G) &= \{e = uv \in E(G) : d_u = 1 \text{ and } d_v = 3\}, \\ E_3(G) &= \{e = uv \in E(G) : d_u = d_v = 2\}, \\ E_4(G) &= \{e = uv \in E(G) : d_u = 2 \text{ and } d_v = 3\}, \\ E_5(G) &= \{e = uv \in E(G) : d_u = 2 \text{ and } d_v = 4\}, \\ E_6(G) &= \{e = uv \in E(G) : d_u = d_v = 3\}. \end{split}$$

Also, we get

 $|E_1(G)| = 9, |E_2(G)| = 33, |E_3(G)| = 42, |E_4(G)| = 69, |E_5(G)| = 12, |E_6(G)| = 27.$ 



Fig. 1. Structure of the first generation dendrimeric chelators (Zhou et al. 2018)

## Theorem 1.

Let G be the first generation dendrimeric chelators. Then the first Zagreb index  $M_1(G)$ , the second Zagreb index  $M_2(G)$ , the second modified Zagreb index  $^mM_2(G)$  and the reduced second Zagreb index  $RM_2(G)$  for G are

- 1.  $M_1(G) = 906$
- 2.  $M_2(G) = 1038$
- $3. \quad {}^mM_2(G) = 42$
- 4.  $RM_2(G) = 324$

## **Proof:**

Using this edge partition of the first generation dendrimeric chelators and by the respective formulas of different versions of the Zagreb indices, we get

$$\begin{aligned} 1. \quad &M_1(G) = \sum_{uv \in E(G)} (d_u + d_v) \\ &= |E_1(G)|(1+2) + |E_2(G)|(1+3) + |E_3(G)|(2+2) + |E_4(G)|(2+3) \\ &+ |E_5(G)|(2+4) + |E_6(G)|(3+3) \\ &= 9 \times 3 + 33 \times 4 + 42 \times 4 + 69 \times 5 + 12 \times 6 + 27 \times 6 = 906 \\ 2. \quad &M_2(G) = \sum_{uv \in E(G)} (d_u \times d_v) \\ &= |E_1(G)|(1\times2) + |E_2(G)|(1\times3) + |E_3(G)|(2\times2) + |E_4(G)|(2\times3) \\ &+ |E_5(G)|(2\times4) + |E_6(G)|(3\times3) \\ &= 9 \times 2 + 33 \times 3 + 42 \times 4 + 69 \times 6 + 12 \times 8 + 27 \times 9 = 1038 \\ 3. \quad &^mM_2(G) = \sum_{uv \in E(G)} \frac{1}{d_u d_v} \\ &= |E_1(G)| \frac{1}{1\times2} + |E_2(G)| \frac{1}{1\times3} + |E_3(G)| \frac{1}{2\times2} + |E_4(G)| \frac{1}{2\times3} + |E_5(G)| \frac{1}{2\times4} \\ &+ |E_6(G)| \frac{1}{3\times3} \\ &= \frac{9}{2} + \frac{33}{3} + \frac{42}{4} + \frac{69}{6} + \frac{12}{8} + \frac{27}{9} = 42 \\ 4. \quad &RM_2(G) = \sum_{uv \in E(G)} (d_u - 1) (d_v - 1) \\ &= |E_1(G)|(1-1)(2-1) + |E_2(G)|(1-1)(3-1) + |E_3(G)|(2-1)(2-1) \\ &+ |E_4(G)|(2-1)(3-1) + |E_6(G)|(2-1)(4-1) \\ &+ |E_5(G)|(3-1)(3-1) \\ &= 9 \times 0 + 33 \times 0 + 42 + 69 \times 2 + 12 \times 3 + 27 \times 4 = 324 \end{aligned}$$

## **Remark:**

By observing the structure of the second generation dendrimeric chelators, we inferred six partitions of the edge set as:

$$E_{1}(G) = \{e = uv \in E(G) : d_{u} = 1 \text{ and } d_{v} = 2\}$$

$$E_{2}(G) = \{e = uv \in E(G) : d_{u} = 1 \text{ and } d_{v} = 3\}$$

$$E_{3}(G) = \{e = uv \in E(G) : d_{u} = 2 \text{ and } d_{v} = 3\}$$

$$E_{4}(G) = \{e = uv \in E(G) : d_{u} = d_{v} = 2\}$$

$$E_{5}(G) = \{e = uv \in E(G) : d_{u} = 2 \text{ and } d_{v} = 4\}$$

$$E_{6}(G) = \{e = uv \in E(G) : d_{u} = d_{v} = 3\}$$

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#### Also, we get

 $|E_1(G)| = 10, |E_2(G)| = 25, |E_3(G)| = 100, |E_4(G)| = 95, |E_5(G)| = 16, |E_6(G)| = 27$ 



Fig. 2: Second generation dendrimeric chelators (Zhou et al. 2018).

## Theorem 2.

Let G be the second generation dendrimeric chelators. Then the first Zagreb index  $M_1(G)$ , the second Zagreb index  $M_2(G)$ , the second modified Zagreb index  $^mM_2(G)$  and the reduced second Zagreb index  $RM_2(G)$  for G are

- 1.  $M_1(G) = 1263$
- 2.  $M_2(G) = 1436$
- 3.  ${}^{m}M_2(G) = \frac{355}{6}$
- 4.  $RM_2(G) = 446$

## **Proof:**

Using this edge partition of the second generation dendrimeric chelators and by the respective formulas of different versions of the Zagreb indices, we get

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1. 
$$M_{1}(G) = \sum_{uv \in E(G)} (d_{u} + d_{v})$$

$$= |E_{1}(G)|(1 + 2) + |E_{2}(G)|(1 + 3) + |E_{3}(G)|(2 + 2) + |E_{4}(G)|(2 + 3) + |E_{5}(G)|(2 + 4) + |E_{6}(G)|(3 + 3) = 10 \times 3 + 25 \times 4 + 100 \times 4 + 95 \times 5 + 16 \times 6 + 27 \times 6 = 1263$$
2. 
$$M_{2}(G) = \sum_{uv \in E(G)} (d_{u} \times d_{v})$$

$$= |E_{1}(G)|(1 \times 2) + |E_{2}(G)|(1 \times 3) + |E_{3}(G)|(2 \times 2) + |E_{4}(G)|(2 \times 3) + |E_{5}(G)|(2 \times 4) + |E_{6}(G)|(3 \times 3) = 10 \times 2 + 25 \times 3 + 100 \times 4 + 95 \times 6 + 16 \times 8 + 27 \times 9 = 1436$$
3. 
$${}^{m}M_{2}(G) = \sum_{uv \in E(G)} \frac{1}{d_{u}d_{v}}$$

$$= |E_{1}(G)|\frac{1}{1 \times 2} + |E_{2}(G)|\frac{1}{1 \times 3} + |E_{3}(G)|\frac{1}{2 \times 2} + |E_{4}(G)|\frac{1}{2 \times 3} + |E_{5}(G)|\frac{1}{2 \times 4} + |E_{6}(G)|\frac{1}{3 \times 3}$$

$$= \frac{10}{2} + \frac{25}{3} + \frac{100}{4} + \frac{95}{6} + \frac{16}{8} + \frac{27}{9} = \frac{355}{6}$$
4. 
$$RM_{2}(G) = \sum_{uv \in E(G)} (d_{u} - 1)(d_{v} - 1)$$

$$= |E_{1}(G)|(1 - 1)(2 - 1) + |E_{2}(G)|(1 - 1)(3 - 1) + |E_{3}(G)|(2 - 1)(2 - 1) + |E_{4}(G)|(2 - 1)(3 - 1) + |E_{5}(G)|(3 - 1)(3 - 1)$$

$$= 10 \times 0 + 25 \times 0 + 100 + 95 \times 2 + 16 \times 3 + 27 \times 4 = 446$$

Fig. 3. Dendrimeric chelators containing six hexadentate centres (Zhou et al. 2018)

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By observing the structure of dendrimeric chelators contain six hexadentate centres, we inferred six partitions of the edge set as:

$$E_{1}(G) = \{e = uv \in E(G): d_{u} = 1 \text{ and } d_{v} = 2\},\$$

$$E_{2}(G) = \{e = uv \in E(G): d_{u} = 1 \text{ and } d_{v} = 3\}$$

$$E_{3}(G) = \{e = uv \in E(G): d_{u} = d_{v} = 2\},\$$

$$E_{4}(G) = \{e = uv \in E(G): d_{u} = 2 \text{ and } d_{v} = 3\}$$

$$E_{5}(G) = \{e = uv \in E(G): d_{u} = 2 \text{ and } d_{v} = 4\},\$$

$$E_{6}(G) = \{e = uv \in E(G): d_{u} = d_{v} = 3\}.$$

Also, we get

 $|E_1(G)| = 18, |E_2(G)| = 72, |E_3(G)| = 118, |E_4(G)| = 146, |E_5(G)| = 32, |E_6(G)| = 56$ 



Fig. 4. Dendrimeric chelators containing nine hexadentate centres (Zhou et al. 2018)

#### Theorem 3.

Let G be the dendrimeric chelators contain six hexadentate centres. Then the first Zagreb index  $M_1(G)$ , the second Zagreb index  $M_2(G)$ , the second modified Zagreb index  $^mM_2(G)$  and the reduced second Zagreb index  $RM_2(G)$  for G are

- 1.  $M_1(G) = 2072$
- 2.  $M_2(G) = 2360$
- 3.  ${}^{m}M_2(G) = \frac{1747}{18}$
- 4.  $RM_2(G) = 730$

## **Proof:**

Using this edge partition of the dendrimeric chelators contain six hexadentate centres and by the respective formulas of different versions of the Zagreb indices, we get

$$\begin{split} 1. M_1(G) &= \sum_{uv \in E(G)} (d_u + d_v) \\ &= |E_1(G)|(1+2) + |E_2(G)|(1+3) + |E_3(G)|(2+2) + |E_4(G)|(2+3) \\ &+ |E_5(G)|(2+4) + |E_6(G)|(3+3) \\ &= 18 \times 3 + 72 \times 4 + 118 \times 4 + 146 \times 5 + 32 \times 6 + 56 \times 6 = 2072 \\ 2. M_2(G) &= \sum_{uv \in E(G)} (d_u \times d_v) \\ &= |E_1(G)|(1\times2) + |E_2(G)|(1\times3) + |E_3(G)|(2\times2) + |E_4(G)|(2\times3) \\ &+ |E_5(G)|(2\times4) + |E_6(G)|(3\times3) \\ &= 18 \times 2 + 72 \times 3 + 118 \times 4 + 146 \times 6 + 32 \times 8 + 56 \times 9 = 2360 \\ 3. {}^{m}M_2(G) &= \sum_{uv \in E(G)} \frac{1}{d_u d_v} \\ &= |E_1(G)| \frac{1}{1\times2} + |E_2(G)| \frac{1}{1\times3} + |E_3(G)| \frac{1}{2\times2} + |E_4(G)| \frac{1}{2\times3} + |E_5(G)| \frac{1}{2\times4} \\ &+ |E_6(G)| \frac{1}{3\times3} \\ &= \frac{18}{2} + \frac{72}{3} + \frac{118}{4} + \frac{146}{6} + \frac{32}{8} + \frac{56}{9} = \frac{1747}{18} \\ 4. RM_2(G) &= \sum_{uv \in E(G)} (d_u - 1)(d_v - 1) \\ &= |E_1(G)|(1-1)(2-1) + |E_2(G)|(1-1)(3-1) + |E_3(G)|(2-1)(2-1) \\ &+ |E_4(G)|(2-1)(3-1) + |E_6(G)|(2-1)(4-1) + |E_5(G)|(3-1)(3-1) \\ &= 18 \times 0 + 72 \times 0 + 118 + 146 \times 2 + 32 \times 3 + 56 \times 4 = 730 \end{split}$$

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#### Remark

By observing the structure of dendrimeric chelators contain nine hexadentate centres, we inferred six partitions of the edge set as:

$$E_{1}(G) = \{e = uv \in E(G) : d_{u} = 1 \text{ and } d_{v} = 2\},\$$

$$E_{2}(G) = \{e = uv \in E(G) : d_{u} = 1 \text{ and } d_{v} = 3\}$$

$$E_{3}(G) = \{e = uv \in E(G) : d_{u} = d_{v} = 2\},\$$

$$E_{4}(G) = \{e = uv \in E(G) : d_{u} = 2 \text{ and } d_{v} = 3\}$$

$$E_{5}(G) = \{e = uv \in E(G) : d_{u} = 2 \text{ and } d_{v} = 4\},\$$

$$E_{6}(G) = \{e = uv \in E(G) : d_{u} = d_{v} = 3\}.$$

Also, we get

 $|E_1(G)| = 27, |E_2(G)| = 108, |E_3(G)| = 174, |E_4(G)| = 219, |E_5(G)| = 48, |E_6(G)| = 84$ 

#### Theorem 4.

Let G be the dendrimeric chelators contain nine hexadentate centres. Then the first Zagreb index  $M_1(G)$ , the second Zagreb index  $M_2(G)$ , the second modified Zagreb index  $^mM_2(G)$  and the reduced second Zagreb index  $RM_2(G)$  for G are

- 1.  $M_1(G) = 3096$
- 2.  $M_2(G) = 3432$
- 3.  ${}^{m}M_2(G) = \frac{869}{6}$
- 4.  $RM_2(G) = 1092$

## **Proof:**

Using this edge partition of the dendrimeric chelators contain nine hexadentate centres and by the respective formulas of different versions of the Zagreb indices, we get

1. 
$$M_1(G) = \sum_{uv \in E(G)} (d_u + d_v)$$
  

$$= |E_1(G)|(1+2) + |E_2(G)|(1+3) + |E_3(G)|(2+2) + |E_4(G)|(2+3) + |E_5(G)|(2+4) + |E_6(G)|(3+3)$$

$$= 27 \times 3 + 108 \times 4 + 174 \times 4 + 219 \times 5 + 48 \times 6 + 84 \times 6 = 3096$$
2.  $M_2(G) = \sum_{uv \in E(G)} (d_u \times d_v)$ 

 $\begin{aligned} &= |E_1(G)|(1 \times 2) + |E_2(G)|(1 \times 3) + |E_3(G)|(2 \times 2) + |E_4(G)|(2 \times 3) \\ &+ |E_5(G)|(2 \times 4) + |E_6(G)|(3 \times 3) \end{aligned}$   $&= 27 \times 2 + 108 \times 3 + 174 \times 4 + 219 \times 6 + 48 \times 8 + 84 \times 9 = 3432$ 3.  ${}^{m}M_2(G) = \sum_{uv \in E(G)} \frac{1}{d_u d_v}$   $&= |E_1(G)| \frac{1}{1 \times 2} + |E_2(G)| \frac{1}{1 \times 3} + |E_3(G)| \frac{1}{2 \times 2} + |E_4(G)| \frac{1}{2 \times 3} + |E_5(G)| \frac{1}{2 \times 4} + |E_6(G)| \frac{1}{3 \times 3}$   $&= \frac{27}{2} + \frac{108}{3} + \frac{174}{4} + \frac{219}{6} + \frac{48}{8} + \frac{84}{9} = \frac{869}{6}$ 4.  $RM_2(G) = \sum_{uv \in E(G)} (d_u - 1)(d_v - 1)$   $&= |E_1(G)|(1 - 1)(2 - 1) + |E_2(G)|(1 - 1)(3 - 1) + |E_3(G)|(2 - 1)(2 - 1) + |E_4(G)|(2 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(2 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(3 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_5(G)|(3 - 1)(4 - 1) + |E_6(G)|(3 - 1)(4 - 1) + |E_6(G)|(3 - 1)(3 - 1) + |E_6(G)|(3 - 1)(4 - 1) + |E_6(G)|(3 - 1)(4 - 1) + |E_6(G)|(3 - 1)(4 - 1) + |E_6(G)|(4 - 1)(4 - 1) + |E_6(G)|(4$ 

# 4 Conclusions

In this work, we considered, hexadentate 3-hydroxypyridinones-terminated dendrimers which are used in iron binding and anti-microbial activities. We calculated the four different versions of the Zagreb indices of these four novel hexadentate 3-hydroxypyridinone-terminated dendrimers which have been demonstrated to have a high affinity towards iron (III) ions and have the antimicrobial property. These indices are calculated by using the edge set partitions of these structures of dendrimers.

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